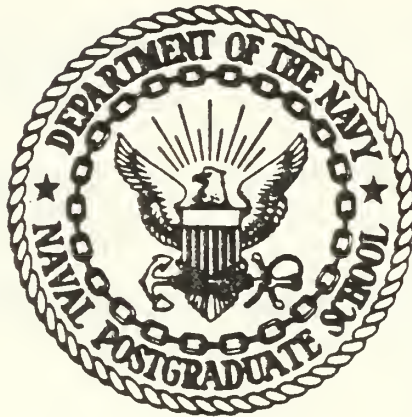# NAVAL POSTGRADUATE SCHOOL
Monterey, California

THESIS

NUMERICAL OPTIMIZATION USING DESKTOP COMPUTERS

by

Walter Bacon Cole

September 1980

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REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) Numerical Optimization Using Desktop Computers		5. TYPE OF REPORT & PERIOD COVERED Master's Thesis; September 1980
		6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(s) Walter Bacon Cole		8. CONTRACT OR GRANT NUMBER(s)
9. PERFORMING ORGANIZATION NAME AND ADDRESS Naval Postgraduate School Monterey, California 93940		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
11. CONTROLLING OFFICE NAME AND ADDRESS Naval Postgraduate School Monterey, California 93940		12. REPORT DATE September 1980
		13. NUMBER OF PAGES 164 pages
14. MONITORING AGENCY NAME & ADDRESS(if different from Controlling Office)		15. SECURITY CLASS. (of this report) Unclassified
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE

16. DISTRIBUTION STATEMENT (of this Report)

Approved for public release; distribution unlimited.

17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)

18. SUPPLEMENTARY NOTES

19. KEY WORDS (Continue on reverse side if necessary and identify by block number)

Numerical optimization, desktop computers, energy conversion, nonimaging solar collectors

20. ABSTRACT (Continue on reverse side if necessary and identify by block number)

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(Page 1) S/N 0102-014-6601

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design of stated thermal capacity. NISCO was coupled to the OPCON/
DESOP optimization program to find the design which maximizes the
life-cycle fuel savings.

Numerical Optimization Using Desktop Computers

by

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Submitted in partial fulfillment of the
requirements for the degree of

MASTER OF SCIENCE IN MECHANICAL ENGINEERING

from the

NAVAL POSTGRADUATE SCHOOL
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NOMENCLATURE

English Letter Symbols

A_r — Solar collector receiver surface area

A_t — One half the solar collector aperature area

B — Cantilevered beam width

C_d — Solar collector depth

C_p — Specific heat

CR — Solar collector concentration ratio

E — Young's modulus of elasticity, or the penalty function exponent used in DESOP

F_1 — Lower Golden Section fraction

F_2 — Upper Golden Section fraction

H — Cantilevered beam height

$\bar{H}$ — Equality constraint vector

Icalc — A user's flag in the DESOP program for initial and final user generated output

L — Cantilevered beam length, or the solar collector length

$\dot{m}$ — Solar collector mass flow rate

Mfr — Solar collector mass flow rate

Ndv — Number of design variables

Obj — Objective function

Opj — Penalized objective function

P — Cantilevered beam load

Qa — Solar collector heat available

Qu	– Solar collector heat gain
Qy	– Yearly solar collector heat available
q_i	– Heat flux
R	– Penalty parameter used in DESOP or the solar collector receiver radius
r	– Solar collector receiver radius
Tap	– Solar collector aperature cover temperature
Tc2	– Solar collector coolant exit temperature
Thetai	– Solar collector acceptance half angle
Thetat	– Solar collector truncation angle
t	– Solar collector distance between the reflector and a point tangent to the receiver
V	– Cantilevered beam volume
x	– Solar collector reflector coordinate
$\bar{X}$	– Design variable vector
y	– Solar collector reflector coordinate

Greek Letter Symbols

α	– One-dimensional search move parameter
δ	– Cantilevered beam deflection
Θ	– Solar collector geometry angle measured from the collector centerline (See Fig. 6)
Θ_i	– Solar collector acceptance half angle
Θ_t	– Solar collector truncation angle
ν	– Cantilevered beam shear stress
σ_b	– Cantilevered beam bending stress

ACKNOWLEDGEMENT

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I. INTRODUCTION

A. BACKGROUND

Most engineering design problems contain several continuous variables and as such have an infinite number of solutions. The purpose of optimization is to find the best possible solution among the many potential solutions for a given problem in terms of some effectiveness or performance criteria. There are several methods of optimization. The methods may be classified as follows:

Analytical methods which use the classical techniques of differential calculus and the calculus of variations.

Numerical methods which use past information to generate better solutions to the optimization problem by means of iterative procedures. Numerical methods can be used to solve problems that cannot be solved analytically.

Graphical methods which use the preparation of a plot of the parameter to be optimized as a function of one or more variables. This method although simple and easy to use becomes unmanageable when there are three or more design variables.

Experimental methods which use direct experimentation of the actual process, the results of one experiment being used to decide on where to perform the next experiment.

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Case study methods which evaluate the results from a number of representative cases, and choose the "best" solution. The "best" solution is thus not likely to be the optimum solution.

Of the optimization methods, the numerical method lends itself to computerized solution. As design is an interactive process between the designer and the problem, and the desktop computer lends itself towards dedicated interactive use, the development of a numerical optimization program for use on a desktop computer in an interactive mode, is the objective of this thesis.

To date a great amount of effort has been spent developing reliable and efficient optimization programs for mainframe computers. These programs are fairly large and complex, requiring a substantial amount of core space during execution. The size and complexity of the programs has been the result of an attempt to minimize the amount of computer time required to perform an optimization and thus the cost to the user. With the advent and availability of desktop computers, there has been a sharp reduction in the cost of computer time to the computer user. While the desktop computer has far less core space than a mainframe computer, once the time factor is removed from the numerical optimization process it is possible to put a small but reliable numerical optimization program on a desktop computer. A design problem concerning the optimal geometry

for a nonimaging parabolic trough solar collector was developed to demonstrate the engineering application of the numerical optimization program developed for this thesis.

B. SCOPE

The numerical optimization of a given function may be accomplished using many varied and different algorithms. Some of the more popular methods used are: random search, linear programming, feasible directions, Golden Section, Newton's method and sequential unconstrained minimization. A particular optimization program will use one or more of these methods to efficiently and reliably arrive at the best solution to a particular problem.

For this thesis two computer programs were developed to perform numerical optimization on a desktop computer. The first program was developed as an executive program to control the optimization process. The executive program is named OPCON which stands for OPtimizer CONtrol program. OPCON provides the interactive link between the user and the program which performs the numerical optimization. OPCON allows the user to input data, attach a specified analysis subprogram to the numerical optimization program and control execution of the numerical optimization program. The second program developed was the numerical optimization program, DESOP. DESOP stands for DEsktop Sequential uncon-strained minimization technique Optimization Program.

DESOP performs the numerical optimization of the user
supplied problem using the sequential unconstrained mini-
mization technique with an external penalty function. The
unconstrained subproblem is solved using the Fletcher-
Reeves method of conjugate directions, Golden Section
search, and polynomial interpolation.

The third computer program, NISCO, was developed to
model a nonimaging concentrating compound parabolic trough
solar collector using thermophysical, geophysical, optical
and economic analysis to compute a life-cycle cost for a
design with a stated energy capacity. NISCO stands for
NonImaging concentrating compound parabolic trough Solar
COllector.

C. OBJECTIVE

The objective of this thesis was to develop a system
of interactive programs for the Hewlett-Packard 9845A
desktop computer which perform numerical optimization, and
to demonstrate the capability on the design of a nonimaging
concentrating compound parabolic trough solar collector.
Three programs were developed to meet the objective: an
executive program, a numerical optimization program and
a solar collector analysis program.

The purposes of the executive program OPCON are:

1. To provide a primary point of contact for the com-
puter user from which to effect a numerical optimization
on any number of user prepared analysis subprograms.

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2.   To provide a standardized, formatted input for the design variables, side constraints and optimizer control parameters, which is recognizable by all the programs in the numerical optimization package of programs.

3.   To control the operation of the different optimization and design analysis programs within the system through a process of program overlays which maximizes the computer space available for the design analysis program.

4.   To develop a program which is portable to different computers using an advanced BASIC language.

The purposes of the numerical optimization program DESOP are to develop an optimization program that:

1.   Is relialbe in reaching a design optimum, irrespective of the starting point.

2.   Will arrive near the design optimum using default values for the optimizer control variables.

3.   Will allow the user to monitor the optimization process and to change the optimizer control variables to more efficiently and/or more accurately reach the design optimum.

4.   Is portable to different computers using an advanced BASIC language.

The purposes of the solar collector program NISCO are to:

1. Model a nonimaging concentrating compound parabolic trough solar collector using a system of thermophysical, geophysical, optical and economic equations.

2. Arrive at an optimum design for a solar collector given a stated average daily heat gain and a life-cycle period.

II. NUMERICAL OPTIMIZATION

A. THE CONCEPT OF NUMERICAL OPTIMIZATION

Consider the problem of designing the cantilevered beam shown in Figure 1. The design task may be broken down into three major parts. First, the objective of the design must be determined, which in this case is to minimize the weight of the beam required to support the concentrated tip load P. Second, any physical constraints that may effect the design must be determined. Thirdly, any limits which exist on the design variables must be determined. The design problem may then be reduced to a system of equations as follows:

Minimize the volume (V)

$$V = B \cdot H \cdot L$$

. Subject to:

Bending stress (σ_b)

$$\sigma_b = \frac{6 \cdot P \cdot L}{B \cdot H^2} \leq 20000 \text{ psi}$$

Shear stress (ν)

$$\nu = \frac{3 \cdot P}{2 \cdot B \cdot H} \leq 10000 \text{ psi}$$

Deflection under load (δ)

$$\delta = \frac{4 \cdot P \cdot L^3}{E \cdot B \cdot H^3} \leq 1 \text{ inch}$$

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Figure 1. Cantilevered Beam Design Problem

With geometric constraints such that:

$$0.5 \leq B \leq 0.5$$

$$1.0 \leq H \leq 20.0$$

$$H/B \leq 10.0$$

At this time the following definitions are introduced:

Objective Function - The parameter which is to be minimized or maximized during optimization. The objective function always occurs on the left side of the equation unless it is also used as a design variable. An objective function may be either linear or nonlinear, implicit or explicit, but must be a function of the design variables.

Design Variable - Any parameter which the optimization process is allowed to change in order to improve the design. Design variables appear only on the right hand side of equations in the analysis program.

Inequality Constraint - Any parameter which must not exceed specified bounds for the design to be acceptable. Constraint functions always appear on the left side of equations. A constraint may be linear, nonlinear, implicit or explicit, but must be a function of one or more design variables.

Equality Constraint - Any parameter which must equal a specified value for the design to be acceptable. The same rules apply to equality constraints as inequality constraints.

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Side Constraint - Any upper or lower bound placed upon a design variable. Side constraints are usually not included in the system of equations that comprise an analysis program. Instead they are usually included as part of the data input to the optimization program.

Analysis Code - The system of equations utilizing the design variables which are used to calculate the objective function and the constraints of a particular design problem.

The general optimization problem may thus be stated mathematically as:

Find the set of design variables $\bar{X}_i$ where $i = 1, 2, \ldots, n$ which will:

Minimize the objective function (Obj)

$$Obj = f(\bar{X})$$

Subject to:

Inequality constraints (G)

$$G_j(\bar{X}) \leq 0 \qquad j = 1, 2, \ldots, m$$

Equality constraints (H)

$$H_j(\bar{X}) = 0 \qquad j = 1, 2, \ldots, l$$

Side constraints

$$X_i^l \leq X_i \leq X_i^u \qquad i = 1, 2, \ldots, n$$

Returning to the cantilevered beam problem, it may be stated in the standard format as follows:

Let $X(1) = B$, $X(2) = H$, and $Obj = Vol = B \cdot H \cdot L$

Then minimize $Obj = Vol$

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Subject to:

$$G(1) = \frac{\sigma_b}{20000} - 1 \leq 0$$

$$G(2) = \frac{\tau}{10000} - 1 \leq 0$$

$$G(3) = \delta - 1 \leq 0$$

$$G(4) = \frac{H}{B} - 10 \leq 0$$

With side constraints:

$$X(1)^l = 0.5$$
$$X(1)^u = 5.0$$
$$X(2)^l = 1.0$$
$$X(2)^u = 20.0$$

It is thus fairly simple and straightforward to perform
an analysis on a particular beam for a given B and H.
Successive analyses may be performed on the cantilevered
beam by solving the above system of equations. It is de-
sirable to automate the successive solutions and to direct
the solutions such that each solution is a better design
than the last. One approach for doing so, and the one
used by DESOP is to proceed as follows: Start with initial
values for B and H. Solve the above set of equations to
find the objective function Obj and to see if any constraints
are violated. A pseudo objective function is created to
represent designs when constraints are violated. If a
constraint is violated, a penalty is added to Obj to form
a penalized objective function Opj. The gradient of the

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penalized objective function at the initial design may be
found by taking the first partial derivative of Opj with
respect to the design variables. The gradient of the
penalized objective function defines the direction of
steepest ascent. In the case of the cantilevered beam, it
is desired to minimize the objective function; therefore,
the greatest improvement in design may be achieved by moving
in the negative gradient, or steepest descent direction.
From the initial design point a search is performed in the
steepest descent direction for the minimum value of Opj in
that direction. At the new minimum, the gradient of the
penalized objective function is again determined and a
search is performed in a conjugate direction until a second
minimum is found. Successive iterations are performed
until the gradient is found to be zero or each successive
iteration produces a sufficiently small change in Opj such
that for all practical purposes the minimum has been found.
At this time the penalty function is increased. If the
design is in a region where there are no constraints
violated an increase in the penalty function will not
change the value of Opj. If on the other hand the design
is in an infeasible region where there are one or more
constraints violated, Opj will be increased, and the
search for a new minimum will commence. If the minimum
of the objective function exists in the infeasible region,

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the minimum value for the objective function in the feasible region will be approached from the infeasible region as the penalty function is increased. The design improvement process will terminate when a zero gradient is found or successive iterations produce a sufficiently small change in the value of Opj and an increase in the penalty function causes no change in Opj.

The minimum thus reached by the optimization process is a minimum with respect to the penalized objective surface immediately surrounding the final design point. The optimization process cannot distinguish between local and global minimum points. It is thus good engineering practice to run several optimizations for a particular design problem from several different initial design points. If optimizations performed from different initial design points converge on the same minimum point, that point is probably a global minimum. If on the other hand two or more minimums are found, there may be local minimums located in the design space being considered and care must be taken to find the global minimum.

B. THE DESOP NUMERICAL OPTIMIZATION PROGRAM

The DEsktop Sequential unconstrained minimization technique Optimization Program was developed using the basic optimization approach outlined in Section II.A. A copy of the program is included in Appendix E. The major

program structure is shown in Figure 2. The following discussion will refer to Figure 2 and describe the major features of the program.

1. Basic Program Execution

The DESOP program begins execution when it is loaded, linked to the user's analysis subprogram, and the program is instructed to run by the OPCON program. The above actions are automatically performed by the OPCON program. DESOP is loaded into the computer by an overlay process. Therefore no variables can be directly transferred between the DESOP and OPCON programs. DESOP begins execution by reading the optimizer control variables and the design variables that were input using the OPCON program and saved to a mass storage device. The program then sets Icalc equal to one and evaluates the objective function and constraints at the initial design point. Icalc is a flag provided the user to key user specified output on the initial and final design analysis. DESOP will provide the user with a hard copy output of the initial design variables, the value of the constraints, the objective function and the penalized objective function. The user then has the option of continuing with the DESOP program to optimize his analysis subprogram or to return to the OPCON program to change one or more of the input parameters.

Figure 2.   DESOP Flow Diagram

Proceeding with the optimization, there are two major loops in the optimization program. The outer loop increases the penalty function when the inner loop's convergence criteria have been met. A convergence test is then performed by the outer loop. If the convergence criteria is met, the optimization process is considered finished. If the convergence criteria for the outer loop is not met, program execution is returned to the inner loop. The inner loop performs successive iterations searching for the minimum of the penalized objective function with no increase in the penalty function taking place. When the inner loop's convergence criteria have been met program execution is transferred to the outer loop.

Execution of the program while in the inner loop proceeds as follows: First, the gradient of the penalized objective function is calculated by subroutine GRAD. The program then computes a search direction using either a steepest descent method or the method of conjugate directions developed by Fletcher and Reeves [Ref. 1]. Once a search direction is established the optimizer attempts to locate the minimum value of the penalized objective function in the search direction. This process if referred to as the one-dimensional search and is illustrated in Figure 3. The efficiency and accuracy to which the one-dimensional search for the minimum of the penalized objective function

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Figure 3. The One-Dimensional Search Process

EXPANDING SEARCH FOR THE MINIMUM

$\alpha z^1 \quad \alpha 3^1$
$\alpha z^2 \quad \alpha 1^2 \quad \alpha 3^2$
$\alpha z^3 \quad \alpha 1^3$

MINIMUM BRACKETED – GOLDEN SECTION SEARCH TO LOCALIZE THE MINIMUM

$\alpha z^4 \quad \alpha 1^4 \quad \alpha 2^4$
$\alpha z^5 \quad \alpha 1^5 \quad \alpha 2^5 \quad \alpha 3^5$
$\alpha 1^6 \quad \alpha 2^6 \quad \alpha 3^6$
αz^6

$Opj1^4 < Opj2^4$

$Opj1^5 > Opj2^5$

Opj

α

$0 \quad 6 \quad 15.7 \quad 21.7 \quad 25.4 \quad 27.8 \quad 31.4 \quad 41.4$

$\alpha 3^3 \quad \alpha 3^4$

is accomplished, is the key to successful sequential un-constrained minimization technique numerical optimization. The one-dimensional problem may be expressed in terms of the penalized objective function, Opj, and the amount of movement, α, in the search direction, $\bar{S}$. First the slope of Opj with respect to α is calculated. An initial "guess" of how far to move is made using subroutine ALPGES. The α which corresponds to the minimum value of Opj in the one-dimensional search is then calculated using subroutine ALPBND and subroutine QUEBIC. The minimum value of Opj thus found is then compared to the previous value of Opj for convergence using subroutine CONVRG. If convergence is not met, execution returns to the start of the inner loop. If convergence is met, execution returns to the outer loop.

When the convergence criteria have been met for both the inner and outer loops, the program proceeds to set Icalc to three as a flag for user generated output for the final design. DESOP then provides the user with a hard copy output of the final design variables, objective function value, penalized objective value, constraint values, the number of inner loop iterations, the number of times the analysis subprogram was called and the final value of the penalty function. The OPCON program is then overlayed over the DESOP program and program execution is returned to the OPCON program.

2. Finding the Search Direction

The first step in finding the search direction, $\bar{S}$, is to determine the slope of Opj at the present design point. The forward finite difference method is used.where:

$$\frac{\partial F}{\partial X_i} = \frac{F(X_i + \Delta X_i) - F(X_i)}{\Delta X_i} = -S_i$$

$$i = 1, 2, \ldots Ndv$$

As $\partial F / \partial X_i$ gives the direction of positive slope, the search direction is the negative of $\partial F / \partial X_i$. The first search is performed using the steepest descent as found above using the following relation:

$$X_i' = X_i + \alpha S_i$$

where alpha is the distance moved in the $\bar{S}$ direction. When a minimum is obtained along the direction of steepest descent, a new Fletcher-Reeves conjugate search direction [Ref. 1] is calculated at the new Design point using the following relations:

$$S_i' = \frac{\partial F}{\partial X_i} + BS_i$$

$$B = \frac{\sum_{i=1}^{Ndv} [\frac{\partial F'}{\partial X_i}]^2}{\sum_{i=1}^{Ndv} [\frac{\partial F}{X_i}]^2}$$

where the prime denotes values for the present iteration and the non-prime variables indicate values for the previous

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iteration. A one-dimensional search is then performed in the new search direction. Searches are continued using the conjugate direction method for Ndv + 1 iterations, where Ndv is the number of design variables. The search process is then restarted using the steepest descent method. The reason for incorporating the conjugate search method is that the steepest descent method when traversing a design surface with a curved valley will tend to zigzag from one side of the design surface valley to the other making very little progress as is illustrated in Figure 4. The conjugate direction method is much more efficient in traversing such a design surface. However, as the conjugate direction method is additive upon previous searches, it has a tendency to decrease in effectiveness with each successive search owing to the accumulation of numerical "noise." For that reason the search process is restarted with the steepest descent method every Ndv + 1 iterations, or when the conjugate direction predicts a positive slope. The search direction is normalized to avoid inaccuracies caused by numerical ill-conditioning.

3. Estimating an Initial Value for Alpha

The initial estimate for alpha is made in the following manner: First, the slope of Opj in the search direction is calculated as the sum of each of the products of the gradients times the search direction. Then the slope of Opj in the search direction is divided by the value

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Figure 4. Steepest Descent and Conjugate Direction Search in a Two-Dimension Design Space.

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of Opj. This value is then multiplied by an improvement

percentage in Opj. This first estimate is then applied to

a series of conditional tests to determine the validity of

the estimate with respect to the slope of Opj and the magni-

tude of the design variables. Lastly, the estimate for

alpha is checked to see if it violates any side constraints.

If it does, the value of the estimate for alpha is reduced

until the side constraints are no longer violated.

4. Calculating Alpha

The calculation of alpha is the most critical al-

gorithm in the DESOP program in providing reliable optimizer

operation. The ability to accurately and efficiently find

the minimum of the penalized objective function in the one-

dimensional search affects directly the operation of the

optimizer. Figure 5 illustrates the zigzag phenomenon

which occurs if alpha is not accurately found. The zigzag

phenomenon is caused by the fact that the optimizer in per-

forming the forward finite difference for calculating the

search direction perturbs the design vector a very small

amount. As such the optimizer can only "see" the design

surface that is immediately adjacent to the design point.

Therefore, if the minimum is not found in the one-dimensional

search, the optimizer will converge very slowly on the

minimum.

There are two major sections to the ALPBND subroutine.

The first section attempts to find the minimum value of Opj

Figure 5.   The Zigzag Phenomenon

using an expanding search technique. The first move is the amount predicted by the ALPGES subroutine. If the minimum is not bracketed by the first move, additional moves are made. Each move is larger than the last. The size of the move is increased each time by an amount equal to the size of the last move divided by the lower Golden Section fraction, where the Golden Section fractions are:

$$F_1 = \frac{3 - \sqrt{5}}{2}$$

$$F_2 = \frac{\sqrt{5} - 1}{2}$$

The lower Golden Section fraction, F_1, is used so that the interval will be consistent with the Golden Section search in the second section of the ALPBND subroutine. The expanding search is continued until the minimum value of the objective function has been bracketed.

Once the minimum is bracketed, a Golden Section search is performed to reduce the bracketing interval on the minimum by an amount such that when the two end points of the interval are taken with two points internal to the interval and a cubic is passed through the four points, the cubic will accurately predict the minimum of the penalized objective function. Himmelblau in [Ref. 2] states that the Golden Section search method of reducing the interval around the minimum of Opj is the most effective of the reducing techniques studied. Golden Section search is based

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on the splitting of a line into two segments known in ancient times as the "Golden Section." The ratio of the whole line to the larger segment is the same as the ratio of the larger segment to the smaller segment. The two Golden Section fractions are employed to split the interval bracketing the minimum as shown in Figure 3. Once the interval has been split, the two values of Opj corresponding to the internal points are compared to find the larger of the two. The internal point with the larger value of Opj will become the new end point for the interval, the remaining interior point will by the fact that it was determined by a Golden Section fraction, be equal to the point determined by the other Golden Section fraction. Thus, only one new point must be calculated to continue the Golden Section search. The search is continued in this manner until the vertical separation of the two end points with respect to the interior points is less than one percent. The four values of the penalized objective function corresponding to the four Golden Section search points are then sent to a cubic interpolator. The cubic interpolator will return a value for alpha to predict the minimum of the penalized objective function, and the minimum of the cubic function that the interpolator has created. The subroutine ALPBND will then test the predicted minimum with the minimum found at the predicted alpha. If there is less than a tenth of

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one percent difference between the two values of the objective function, the point predicted by the cubic interpolator will be accepted as the minimum and program execution will return to the main program. If the predicted minimum is not sufficiently close to the minimum at the predicted alpha, another Golden Section search will be performed to reduce the interval and better localize the minimum. The four points from the reduced interval will then be sent to the cubic interpolation subroutine. This process will continue until either the test for the minimum is positive or the interval has been reduced to less than 1E-12. Program execution will then return to the main program.

5. Subroutine QUEBIC

Subroutine QUEBIC is used to estimate the alpha at which Opj is a minimum based on four point cubic interpolation. If the function more closely resembles a quadratic than a cubic, a three point quadratic interpolation is performed using the three points which bracket the minimum. If the predicted minimum is outside the interval spanned by the two end points again a quadratic interpolation is performed. If the minimum still lies outside the two end points, the analysis returns to subroutine ALPBND, the inverval bracketing the minimum is reduced, and program execution returns to QUEBIC.

6. <u>Convergence of the Penalized Objective Function</u>

The penalized objective function is tested for convergence at the end of each inner loop and again at the end of the outer loop in the main program. Convergence is tested by calling subroutine CONVRG. There are two criteria used for testing for convergence. The first tests the relative difference of the value of Opj from the present iteration with the value of Opj from the last iteration. The second method tests the absolute difference of the two values. The second method is employed for cases when the value of the penalized objective function approaches zero. When convergence has been met on two successive iterations, the penalty function is increased by an amount specified by the user in the executive OPCON program. The penalized objective function is again tested for convergence. If convergence is still met, the optimizer considers the present value of the penalized objective function to be a minimum, noting again that numerical optimization programs cannot differentiate between local and global minimums.

7. <u>The Penalty Function</u>

The purpose of the penalty function is to increase the value of the objective function when the design is in an infeasible region. The infeasible region is that region where one or more design constraints are violated. When a constraint is violated, the value of the particular constraint,

G_j, is positive. The objective function is then penalized as follows:

$$Opj = Obj + R \cdot G_j^{E}$$

where:

R - a multiplication constant

E - an exponent constant

This type of penalty function, one where the penalty is applied after the design leaves the feasible region, is known as an exterior penalty function. The exterior type of penalty function was chosen over other types, such as the interior or extended interior penalty function. If a function is discontinuous within the design space being studied, numerical difficulties may be encountered which make performing an optimization of the design difficult.

III. SOLAR COLLECTOR OPTIMIZATION

A. THE CONCEPT OF NONIMAGING SOLAR COLLECTORS

At the present time there are numerous schemes for
the collection of solar energy and its conversion to a more
useful form of energy. In the field of solar collectors
there are three broad categories: flat plate collectors,
focusing collectors and nonimaging collectors. The advan-
tages and disadvantages of each type are shown in Table I.
Welford and Winston in [Ref. 3] report that "in the mid-
1960's, it was realized in at least three different labora-
tories that light could be collected and concentrated for
many purposes, including solar energy, more efficiently by
nonimaging optical systems than by conventional image
forming systems. The methodology of designing optimized
nonimaging systems differs radically from conventional
optical design. The new collectors approach very closely
the maximum theoretical concentration; and for two-dimensional
geometry, which is important for solar energy collection,
this limit is actually reached."[1] Figure 6 shows the basic
geometry for the nonimaging compound parabolic concentrating

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[1] Welford, W. T. and Winston, R., The Optics of Nonimaging
Concentrators, Light and Solar Energy, p. ix, Academic Press,
1978.

TABLE I

Collector Type Advantages and Disadvantages

COLLECTOR TYPE	ADVANTAGES	DISADVANTAGES
FLAT PLATE	Low initial cost Easy to manufacture Utilizes both direct and diffuse radiation No guidance required Good durability Low maintenance	Max. temperature 80°C Large start up losses Large convective and thermal radiation losses
FOCUSING	Max. temperature 200→3000C Low startup losses Low convective and thermal radiation losses	High manufacturing cost due to requirement for highly specular reflecting surfaces Require accurate tracking Maintenance high as reflective surface remains uncovered Does not accept diffuse radiation
NONIMAGING	Accepts both diffuse and direct radiation No tracking required Reflective surface covered Moderate convective and radiation losses Moderate manufacturing costs performance improved by slight imperfections in specular reflection Moderate operating temperatures 80→300C	

Figure 6.   Nonimaging Concentrating Solar Collector
            Geometry

collector. Welford and Winston [Ref. 3] have shown that the
concentration for a maximum input acceptance half-angle,
θ_i, is obtained in two sections. The first section, that
shadowed from the direct rays at angles less than θ_i is an
involute of the receiver cross section. The second section
is such that rays at θ_i are tangent to the receiver after
one reflection at the reflector surface. The x-y coordinates
of a point on the reflector surface for a collector with a
circular receiver may be expressed as:

$$x = -r \cdot \cos\theta + t \cdot \cos(\theta + \pi/2)$$

$$y = r \cdot \sin\theta - t \cdot \sin(\theta + \pi/2)$$

where for $\pi/2 + \theta_i \leq \theta \leq 3\pi/2 - \theta_i$

$$t = \frac{r((\theta + \theta_i + \pi/2) - \cos(\theta - \theta_i))}{1 + \sin(\theta - \theta_i)}$$

and for $\theta \leq \theta_i + \pi/2$

$$t = r \cdot \theta$$

r - receiver radius

θ - an angle measured from the collector centerline
as shown in Figure 6.

The concentration ratio, CR, of the collector is defined as
the aperature area of the collector, $2A_c$, divided by the
surface area of the receiver. For the collector shown

$$CR = \frac{2A_c}{2\pi r} .$$

The collector depth, Cd, is used in the economic analysis of collector cost. The truncation angle, θ_t, is the maximum θ used in determining the collector geometry for the truncated collector. The collector may be significantly truncated before any appreciable change in the concentration ratio is affected. This allows a savings in manufacturing costs with little degradation in collector performance.

The nonimaging concentrating solar collector will accept and deliver to the absorber all incident radiation that falls on the collector aperature and that is within the maximum acceptance half angles, θ_i. That is, there is an arc of sky, $2\theta_i$, from which all radiation, direct, diffuse and reflected, is delivered to the absorber. It is this fact which makes the nonimaging concentrating collector attractive for solar energy use. Figures 7, 8, and 9 show ray paths for a nonimaging, truncated collector for the following cases: In Figure 7 the solar altitude is within the acceptance half angles. In Figure 8 the solar altitude is equal to the acceptance half angle. In Figure 9 the solar angle is less than the acceptance half angle. In Figure 7, all the radiation that enters the collector is delivered to the absorber tube and is somewhat scattered over the absorber surface. In Figure 8 again all the radiation that enters the collector is delivered to the absorber tube, but is now tangent to the tube and is concentrated on the front edge of the absorber tube. In

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Figure 7. Ray Path Drawing for Solar Altitude Within the
Maximum Acceptance Half Angle

Figure 8. Ray Path Drawing for Solar Altitude Equal to
the Maximum Acceptance Half Angle

Figure 9.   Ray Path Drawing for Solar Altitude Outside the
Maximum Acceptance Half Angle

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Figure 9 all the reflected radiation leaves the collector, thus the acceptance half angle provides a very sharp cutoff angle for accepting incident radiation.

B. SOLAR COLLECTOR DESIGN PROGRAM

A NonImaging compound parabolic trough Solar COllector hereafter referred to as NISCO was chosen to model in the analysis program. There are seven major heat flow paths considered in the program. The major heat flow paths are shown in Figure 10 and are outlined below:

q_1 - The sum of the direct, diffuse and ground reflected radiation that is incident on the collector cover.

q_2 - The sum of the direct, diffuse and ground reflected radiation that is reflected by the collector cover.

q_3 - The sum of the direct, diffuse and ground reflected radiation that is absorbed by the collector cover.

q_4 - The sum of the direct, diffuse, and ground reflected radiation that is transmitted by the cover and delivered either directly or indirectly to the absorber and is absorbed by the absorber.

q_5 - The sum of the radiation reflected by the absorber that is absorbed by the cover and the thermal radiative and convective exchanges between the absorber and the cover.

q_6 - The sum of the thermal radiative and the convective exchanges between the cover and the environment.

q_7 - The energy delivered to the collector coolant.

Figure 10.   Basic Solar Collector Heat Paths

To determine the energy balance on the collector, a procedure outlined by Kreith and Kreider, [Ref. 6] is followed. All important heat fluxes are first calculated from basic heat-transfer principles. The fluxes are then combined in heat-balance equations for the receiver, the aperature cover, and the coolant fluid. Since the various flux terms are nonlinear in temperature a simultaneous iterative solution is used to solve the equations. Note that the first page of Appendix G is a cross reference list of the major equations used in the subprogram NISCO and the sources used to obtain the equations.

The following discussion will detail the procedure used in the NISCO subprogram to calculate the heat gain for a particular solar collector design and the resultant life-cycle fuel savings. Variable names and program line numbers correspond to those used in the NISCO subprogram. The design variables chosen for the NISCO subprogram were: (1) Thetai, (θ_i), the maximum acceptance half angle, (2) Thetat, (θ_t), the truncation angle, (3) R, (r), the receiver radius, (4) L, the collector length, and (5) Mfr, ($\dot{m}$), the coolant mass flow rate. The objective function of the NISCO subprogram is the life-cycle fuel savings of the collector. Life-cycle fuel savings are calculated as the cost savings realized by the collector over purchasing natural gas per unit quantity of 10^6 Btu's expressed in present worth using the present worth analysis described by Newnan in [Ref. 13]. The constraints

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placed upon the design by the NISCO subprogram were: the maximum and minimum values allowed for the truncation angle due to collector geometry as specified in Section III.A., the mass flow rate of the coolant must be positive, the receiver radius must be positive, a minimum average daily heat gain, and a maximum allowable coolant temperature. The side constraints placed upon the design to ensure that the final design was a reasonable design were: the maximum acceptance half angle must be greater than three degrees but less than 85 degrees, the truncation angle must be greater than 185 degrees but less than 260 degrees, the receiver radius must be greater than one tenth inch but less than two inches, the collector length must be greater than five feet but less than 100 feet, and the mass coolant flow rate must be greater than five lbm/hr and less than 1000 lbm/hr.

The NISCO analysis subprogram proceeds as follows. A minimum average daily heat gain is specified and entered as Q1 in line 1655. The subprogram is then SAVED and the OPCON/DESOP optimization program run. When DESOP calls the NISCO subprogram, it will pass the design variable vector $\bar{X}$ to the NISCO subprogram. The NISCO subprogram in lines 205 to 225 sets the design variable vector $\bar{X}$ equal to the design variables used in the NISCO subprogram. NISCO then proceeds to read in the constants and data used in the solar collector design. The design specifications

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are summarized in Appendix B. Collector geometry calcula-
tions are then performed in lines 820 to 855 to ascertain
the optical properties of the collector as developed in
[Ref. 3]. An initial receiver and aperature cover tempera-
ture is assumed in lines 865 and 870. Monthly calculations
are then performed to calculate the collector tilt angle,
the minimum accepted solar altitude, the ground angle factor
and sky heat loss constants as specified in [Refs. 5 and 6].
An hourly calculation is then performed to calculate the
angle that the sun makes with the collector aperature cover,
the amount of radiation incident on the collector aperature
cover and the collector cover transmissivity and absorptance
as specified in [Refs. 5 and 6]. The iterative portion of
the analysis then proceeds as follows: First, the heat
transfer coefficients for the collector are calculated as
prescribed in [Refs. 4, 6 and 11], lines 1060 to 1145. Next
a heat balance is performed on the cover as prescribed in
[Ref. 6] and a new collector aperature cover, Tap, is cal-
culated in lines 1155 to 1210. A heat balance is then
performed on the receiver as specified in [Ref. 6] and the
energy passed to the coolant, Qu, is calculated in lines
1225 to 1305. Finally a heat balance is performed on the
coolant as prescribed in [Ref. 6] and the coolant exit
temperature is calculated in lines 1320 to 1365. Knowing
the coolant exit temperature, Tc2, an average receiver

temperature may be calculated and compared to the initial assumed receiver temperature, lines 1375 to 1405. If the new receiver temperature is within a tenth of one percent of the old receiver temperature, the analysis program proceeds to calculate the pumping power required for the collector. If the new receiver temperature is not within the convergence specified, the iterative heat balance process is repeated, setting the aperature cover temperature and the receiver temperature to the new value calculated. The pressure drop through the collector and the power required to pump the coolant through the collector are calculated in lines 1430 to 1480, as specified in [Refs. 6 and 12]. The energy required to pump the coolant through the collector is then subtracted from the energy gained by the collector to calculate the available collector energy, Qa, line 1490. Qa is then summed for each hour that the analysis is performed. As the analysis is performed for one day each month, the summation of the available collector energy is then multiplied by thirty to obtain a yearly heat gain, Qy, line 1590. The cost of an equivalent amount of natural gas is then calculated. Using present worth analysis as described in [Ref. 13], a life-cycle savings is then calculated and the initial manufacturing cost of the collector is calculated and subtracted from the life-cycle savings. This result is then divided by the life-cycle

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useful energy gain by the collector and multiplied by 10^6 to obtain the life-cycle fuel savings used as the objective function for the optimization program. The constraints on the design are then calculated in lines 1660 to 1685. Lines 1710 to 1815 contain printout specifications for the first and the last time that the NISCO subprogram is called by the optimization program. The values of the objective function and the constraints are then passed along with program control back to the optimization program.

IV. <u>RESULTS</u>

A major portion of the thesis work was devoted to the development of a reliable optimization program that would optimize a wide variety of problems. Following the accomplishment of this goal, a subprogram was developed to model a nonimaging concentrating compound parabolic trough solar collector.

A. RESULTS OF THE DESOP PROGRAM DEVELOPMENT

In developing the DESOP numerical optimization program, four standard numerical optimization test problems were used. The four test problems provided a wide variety of different numerical problems with which the optimization program had to deal. The four test problems are listed in Appendix F. A major goal of this thesis was to optimize all four problems using default optimizer control variables. The results of the DESOP program optimizing the four test problems are given in Appendix A. The DESOP program was able to make significant design improvements in all four test problems using default optimizer control parameters. When the optimizer control parameters were adjusted for each individual problem, the DESOP program's performance was improved in all four cases. Further experimenting with the optimizer control parameters could lead to an even better performance of the DESOP program.

B. RESULTS OF THE NISCO SUBPROGRAM

A listing of the NISCO subprogram is included as Appendix G. There are numerous comment statements in the subprogram. The reader is encouraged to look closely at the subprogram. The results of the NISCO subprogram may be found in Appendix B. The first section of Appendix B details the design specifications that were chosen for the solar collector model. Three different daily heat capacities were specified 10000, 30000 and 50000 Btu, and the NISCO subprogram was used to find the optimum design for each. The second section of Appendix B gives the initial design and final designs for the three solar collector capacities. In each case the DESOP program was able to significantly improve the design. The instantaneous efficiencies for the final designs are within a few percent of the instantaneous efficiency reported by Kreith and Kreider [Ref. 6] for a slightly different nonimaging concentrating compound parabolic trough solar collector operating under slightly different atmospheric conditions. It is interesting to note that the larger capacity solar collector had the best instantaneous efficiency and also the highest life-cycle fuel savings. In all three cases the optimum incident acceptance angle was found to be 18.04 - 18.05 degrees and the optimum truncation angle was found to lie within the range of 184.55 to 190.0 degrees.

Due to the fact that the objective function is weakly linked to the design capacity of the solar collector, the final daily heat gain is somewhat higher than the minimum set. If a stronger link were to be established between the solar collector capacity and the objective function, the collector design would be driven closer to the stated minimum daily average heat gain. Also, if the convergence criteria is tightened, the optimizer will take longer to reach the minimum but will reach a final design where the average daily heat gain is closer to the minimum set.

APPENDIX A

DESOP TEST PROGRAM RESULTS

This appendix contains the results of the four test programs that were used to develop the DESOP numerical optimization program. For each design the initial design, the true optimum design, the DESOP results using default control parameters, and the DESOP results using adjusted control parameters are given. The four test programs may be found in Appendix F.

DESOP TEST PROGRAM

ANALIZ Subprogram : BANNA

Initial Design:
    Design Variables:
        $X(1) = -1.2$
        $X(2) = 1.0$
    Objective Function:
        Obj = 10.8
        Opj = 10.8
    Side Constraints Violated:
        N/A
    Constraints Violated:
        N/A

True Optimum:
    Design Variables:
        $X(1) = 1.00$
        $X(2) = 1.00$
    Objective Function:
        Obj = 4.00
        Opj = 4.00
    Side Constraints Violated:
        N/A
    Constraints Violated:
        N/A

DESOP Results:

Default Control Parameters:
    Design Variables:
        $X(1) = 0.768$
        $X(2) = 0.578$
    Objective Function:
        Obj = 4.05
        Opj = 4.05
    Side Constraints Violated:
        N/A
    Constraints Violated:
        N/A
    # of Function Evaluations:
        96

Adjusted Control Parameters
    Design Variables:
        $X(1) = 0.791$
        $X(2) = 0.606$
    Objective Function:
        Obj = 4.047
        Opj = 4.047
    Side Constraints Violated:
        N/A
    Constraints Violated:
        N/A
    # of Function Evaluations:
        91

NOTE: The BANNA subprogram has 2 design variables and no

constraints.

DESOP TEST PROGRAM

ANALIZ Subprogram : Rosen-Suzuki

Initial Design:
    Design Variables:
        $X(1) = 1$
        $X(2) = 1$
        $X(3) = 1$
        $X(4) = 1$
    Objective Function:
        Obj = 31
        Opj = 31
    Side Constraints Violated:
        N/A
    Constraints Violated:
        None

True Optimum:
    Design Variables:
        $X(1) = 0.0$
        $X(2) = 1.0$
        $X(3) = 2.0$
        $X(4) = -1.0$
    Objective Function:
        Obj = 6.00
        Opj = 6.00
    Side Constraints Violated:
        N/A
    Constraints Violated
        None

DESOP Results:

Default Control Parameters
    Design Variables:
        $X(1) = 4.72E-02$
        $X(2) = 0.998$
        $X(3) = 1.98$
        $X(4) = -1.00$
    Objective Function:
        Obj = 6.088
        Opj = 6.093
    Side Constraints Violated:
        N/A
    Constraints Violated:
        $G(3) = 0.000527$
    # of Function Evaluations:
        392

Adjusted Control Parameters
    Design Variables:
        $X(1) = -5.167E-03$
        $X(2) = 1.019$
        $X(3) = 1.999$
        $X(4) = -0.9951$
    Objective Function:
        Obj = 5.9998
        Opj = 6.007
    Side Constraints Violated:
        N/A
    Constraints Violated:
        $G(3) = 0.00232$
    # of Function Evaluations:
        306

NOTE: The Rosen-Suzuki subprogram has four design variables

    and three constraints.

DESOP TEST PROGRAM

ANALIZ Subprogram : TSWAR

Initial Design: True Optimum
    Design Variables: Design Variables:
        X(1) = 25.2   X(1) = 4.538
        X(2) = 2.0   X(2) = 2.400
        X(3) = 37.5   X(3) = 60.00
        X(4) = 9.25   X(4) = 9.300
        X(5) = 6.8   X(5) = 7.000
    Objective Function: Objective Function:
        Obj = 3.51E-08   Obj = -5.26E+06
        Opj = 1.64E-14   Opj = -5.26E+06
    Side Constraints Violated: Side Constraints Violated:
        1   None
    Constraints Violated: Constraints Violated:
        3   None

DESOP Results:

Default Control Parameters: Adjusted Control Parameters:
    Design Variables: Design Variables:
        X(1) = 1.12   X(1) = 1.72
        X(2) = -0.163   X(2) = -1.56E-02
        X(3) = 37.5   X(3) = 37.5
        X(4) = 13.5   X(4) = 12.3
        X(5) = 10.6   X(5) = 9.10
    Objective Function: Objective Function:
        Obj = -7.36E-06   Obj = -6.66E+06
        Opj = -7.36E-06   Opj = -6.65E+06
    Side Constraints Violated: Side Constraints Violated:
        $X(2)_l$ = 1.2 $X(2)_l$ = 1.2
        $X(4)_u$ = 9.3 $X(4)_u$ = 9.3
        $X(5)_u$ = 7.0 $X(5)_u$ = 7.0
    Constraints Violated: Constraints Violated:
        None   G(6) = 138
    # of Function Evaluations: # of Function Evaluations:
        161   69

NOTE: The TSWAR subprogram has five design variables and

       six constraints.

DESOP TEST PROGRAM

ANALIZ Subprogram : T7VAR

Initial Design: True Optimum:
    Design Variables: Design Variables:
        X(1) = 1   X(1) = 3
        X(2) = 1   X(2) = 0
        X(3) = 1   X(3) = 0
        X(4) = 1   X(4) = 1
        X(5) = 1   X(5) = 0
        X(6) = 1   X(6) = 0
        X( ) = 1   X(7) = 0
    Side Constraints Violated: Side Constraints Violated:
        None   None
    Objective Function: Objective Function
        Obj = -203   Obj = -190
        Opj = 1007   Opj = -190
    Constraints Violated: Constraints Violated:
        G(1) = 11   None

DESOP Results:

Default Control Parameters: Adjusted Control Parameters:
    Design Variables   Design Variables:
        X(1) = 1.42   X(1) = 2.69
        X(2) = 0.515   X(2) = -7.60E-04
        X(3) = 0.376   X(3) = 1.04E-02
        X(4) = 0.844   X(4) = 1.82
        X(5) = 2.13E-02   X(5) = 2.89E-03
        X(6) = 9.84E-03   X(6) = 2.91E-03
        X(7) = 0.638   X(7) = 0.113
    Side Constraints Violated: Side Constraints Violated:
        None   1
    Objective Function: Objective Function:
        Obj = -142   Obj = -178.6
        Opj = -142   Opj = -179.1
    Constraints Violated: Constraints Violated:
        None   None
    # of Function Evaluations: # of Function Evaluations:
        302   808

NOTE:. The T7VAR subprogram has seven design variables and one

    constraint.

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NISCO DESIGN RESULTS

DESIGN SPECIFICATIONS

A. GEOGRAPHIC

Location	40 degrees North Lattitude
Solar position and intensity levels	ASHRAE Handbook of Fundamentals standard solar radiation design, Ref.
Wall azimuth angle	0 deg.
Cloud Cover	0 %
Vapor Pressure	3 mm Hg
Tamb	ASHRAE Handbook of Fundamentals daily norms for San Francisco, Ca. Ref.

B. COLLECTOR MATERIALS

RECEIVER   Oxidized Copper
  Absoptivity   0.93
  Thermal Emissivity   0.40
  Reflectivity   0.07

REFLECTOR   Vacuum deposited Aluminum on resin
  Reflectivity   0.89

COVER   Double strength window glass
  Specular Absorptance   ASHRAE standards for D.S. window
  Specular Transmisivity   glass. Ref.
  Absorptance av.   0.03
  Transmittance av.   0.80
  Reflectivity av.   0.17
  Thermal Emissivity   0.94

COOLANT   Therminol 55

  Specific gravity   0.87
  Specific heat† $4.9E\text{-}4*Tr+0.4036$ Btu/(lbm F)
  Viscosity† $6.71955E\text{-}4*(-0.053*Tr+32.3)$ lbm/(ft sec)
  Inlet Temperature   100 deg. F

† Values given as a function of average receiver temperature,
   Tr, in degrees F.

C. ECONOMIC

Life-Cycle   20 years
Fuel Cost (Natural Gas)   8.14 $/ 10^6 Btu
Annual Fuel Inflation Rate   0.11
Monetary Inflation Rate   0.10
Collector Cost   22.5 $/ft^3 Ref. 4

NISCO DESIGN - 10000 Btu/DAY SOLAR COLLECTOR

INITIAL DESIGN
    Design Variables:
        Incident acceptance half angle   25.00 deg
        Truncation angle   230.0 deg
        Receiver radius   0.41 in
        Collector length   20.00 ft
        Coolant mass flow rate   108.7 lbm/hr
    Design Features:
        Concentration ratio   2.20
        Collector aperature area   9.56 ft^2
        Collector depth   4.12 in
        Coolant velocity   0.15 ft/sec
        Average daily heat gain   11,400   Btu
        Maximum coolant temperature   137   deg F
        Instantaneous collector efficiency 0.70
        Initial cost $203.00
        Life-cycle cost savings $7.78 $/10^6$ Btu

FINAL DESIGN
    Design Variables:
        Incident acceptance half angle   18.05 deg
        Truncation angle   190.0 deg
        Receiver radius   0.52 in
        Collector length   18.92 ft
        Coolant mass flow rate   124.3 lbm/hr
    Design Features:
        Concentration ratio   1.65
        Collector aperature area   8.48 ft^2
        Collector depth   1.02 in
        Coolant velocity   0.11 ft/sec
        Average daily heat gain   10,600   Btu
        Maximum coolant temperature   131   deg F
        Instantaneous collector efficiency 0.74
        Initial cost $159.00
        Life-cycle cost savings $8.15 $/10^6$ Btu

NISCO DESIGN - 30000 Btu/DAY SOLAR COLLECTOR

INITIAL DESIGN:
    Design variables:
        Incident acceptance half angle   15.00 deg.
        Truncation angle   230.0 deg.
        Receiver radius   1.00 in.
        Collector length   50.0 ft.
        Coolant mass flow rate   100.0 lbm/hr
    Design features:
        Concentration ratio   2.95
        Collector aperature area   77.35 ft^2
        Collector depth   12.62 in.
        Max. coolant temperature   366.59 F
        Instantaneous collector efficiency   0.64
        Average daily heat gain   83,400   Btu
        Initial cost $1,628.90
        Life cycle savings $7.54 $/10^6$ Btu

FINAL DESIGN:
    Design variables:
        Incident acceptance half angle   18.04 deg.
        Truncation angle   184.55 deg.
        Receiver radius   1.28 in.
        Collector length   26.43 ft.
        Coolant mass flow rate   425.23 lbm/hr
    Design features:
        Concentration ratio   1.54
        Collector aperature area   27.35 ft^2
        Collector depth   1.78 in.
        Coolant velocity   6.04E-02 ft/sec
        Max. coolant temperature   129.4 F
        Instantaneous collector efficiency   0.75
        Average daily heat gain   34,473   Btu
        Initial cost $509.98
        Life-cycle savings $8.19 $/10^6$ Btu

Run time - approx. 5 hours

NISCO DESIGN - 50000 Btu/DAY SOLAR COLLECTOR

INITIAL DESIGN
    Design Variables:
        Incident acceptance half angle   20.00 deg.
        Truncation angle   220.0 deg.
        Receiver radius   1.25 in.
        Collector length   50.00 ft.
        Coolant Mass flow rate   500.0 lbm/hr
    Design Features:
        Concentration ratio   2.28
        Collector aperature area   75.5 ft^2
        Collector depth   9.14 in.
        Coolant velocity   7.51E-02 ft/sec
        Maximum coolant temperature   164.   deg. F
        Instantaneous efficiency   0.72
        Average daily heat gain   91,900   Btu
        Initial cost $1,510.00
        Life-cycle savings $7.96 /$10^6$ Btu

FINAL DESIGN
    Design Variables:
        Incident acceptance half angle   18.04 deg.
        Truncation angle   185.0 deg
        Receiver radius   1.43 in
        Collector length   39.3 ft
        Coolant mass flow rate   986   lbm/hr
    Design Features:
        Con entration ratio   1.55
        Collector aperature area   45.5 ft^2
        Collector depth   2.04 in
        Coolant velocity   0.11 ft/sec
        Maximum coolant temperature   121   deg F
        Instantaneous collector efficiency   0.76
        Average daily heat gain   57,800   Btu
        Initial cost $848.00
        Life-cycle savings $8.21 /$10^6$ Btu

APPENDIX C

DESOP USER'S MANUAL

A.   INTRODUCTION

The numerical optimization package of programs, currently
consisting of OPCON and DESOP, provide the capability for
finding the optimum design of a system mathematically modeled
using multiple variables, on the Hewlett-Packard 9845A desk-
top computer. OPCON is an executive program which provides
the user with the following: a primary point of contact with
the computer from which to access the optimization program
DESOP, a standard formatted input for design variables, side
constraints on the design variables, optimizer control varia-
bles, and organization of the optimization process. DESOP
is a numerical optimization program, which when coupled to
a user supplied design analysis program, will optimize the
design. DESOP will allow the user to monitor the optimiza-
tion process as it is taking place. After monitoring the
optimization process, the user may choose to change the
optimizer control variables and/or his design starting
point to more efficiently or more accurately reach the
design optimum. After an optimization has been performed,
DESOP will reload the OPCON program and return the user to
the OPCON program. The OPCON program will then offer the

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user the following three choices: to optimize the same

design, optimize a different design or terminate the

program.

Figure 11 illustrates the overlay method used in

loading the OPCON and DESOP programs.

PROGRAM OVERLAY STRUCTURE   MASS STORAGE

```
┌──────────────────────────┐        ┌──────────────────┐
│ OPCON                    │        │ OPCON            │
│ ─ ─ ─ ─ ─ ─ ─ ─ ─        │        │                  │
│ Input information        │        ├──────────────────┤
│    to files              │        │ DESOP            │
│      ┌──────────────────────┐     │                  │
│      │ DESOP ─ ─ ─ ─ ─ ─ ─ │     ├──────────────────┤
│      │                      │     │ ANALYSIS #1      │
│      │ Read information     │     │ Subprogram       │
│      │    from files        │     ├──────────────────┤
│      │ ─ ─ ─ ─ ─ ─ ─ ─ ─   │     │ ANALYSIS #1      │
│      │                      │     │ Data Files       │
│      │ Optimization Program │     ├──────────────────┤
│      │                      │     │ ANALYSIS #2      │
│      │                      │     │ Subprogram       │
└──────│                      │     ├──────────────────┤
       │                      │     │ ANALYSIS #2      │
       │ ─ ─ ─ ─ ─ ─ ─ ─ ─   │     │ Data Files       │
       │                      │     ├──────────────────┤
       │ User's               │     │                  │
       │ Design Analysis      │     │                  │
       │ Subprogram           │     ├──────────────────┤
       │                      │     │ ANALYSIS #N      │
       │                      │     │ Subprogram       │
       │                      │     ├──────────────────┤
       │                      │     │ ANALYSIS #N      │
       └──────────────────────┘     │ Data Files       │
                                     └──────────────────┘
```

Figure 11. Basic Program Relationships

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B. THE CONCEPT OF NUMERICAL OPTIMIZATION

Consider the problem of designing the cantilevered beam shown in Figure 1. The design task may be broken down into three major parts. First, the objective of the design must be determined, which in this case is to minimize the weight of the beam required to support the concentrated tip load P. Second, any physical constraints that may effect the design must be determined. Thirdly, any limits which exist on the design variables must be determined. The design problem may then be reduced to a system of equations as follows:

Minimize the volume (V)

$$V = B \cdot H \cdot L$$

Subject to:

Bending stress (σ_b)

$$\sigma_b = \frac{6 \cdot P \cdot L}{B \cdot H^2} \leq 20000 \text{ psi}$$

Shear stress (ν)

$$\nu = \frac{3 \cdot P}{2 \cdot B \cdot H} \leq 10000 \text{ psi}$$

Deflection under load (δ)

$$\delta = \frac{4 \cdot P \cdot L^3}{E \cdot B \cdot H^3} - 1 \text{ inch}$$

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Figure 1.   Cantilevered Beam Design Problem

With geometric constraints such that:

$$0.5 \leq B \leq 0.5$$

$$1.0 \leq H \leq 20.0$$

$$H/B \leq 10.0$$

At this time the following definitions are introduced:

Objective Function - The parameter which is to be minimized or maximized during optimization. The objective function always occurs on the left side of the equation unless it is also used as a design variable. An objective function may be either linear or nonlinear, implicit or explicit, but must be a function of the design variables.

Design Variable - Any parameter which the optimization process is allowed to change in order to improve the design. Design variables appear only on the right hand side of equations in the analysis program.

Inequality Constraint - Any parameter which must not exceed specified bounds for the design to be acceptable. Constraint functions always appear on the left side of equations. A constraint may be linear, nonlinear, implicit or explicit, but must be a function of one or more design variables.

Equality Constraint - Any parameter which must equal a specified value for the design to be acceptable. The same rules apply to equality constraints as inequality constraints.

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Side Constraint - Any upper or lower bound placed
upon a design variable. Side constraints are usually not
included in the system of equations that comprise an
analysis program. Instead they are usually included as
part of the data input to the optimization program.

Analysis Code - The system of equations utilizing
the design variables which are used to calculate the objective
function and the constraints of a particular design problem.

The general optimization problem may thus be stated
mathematically as:

Find the set of design variables $\bar{X}_i$ where $i = 1,2,\ldots,n$
which will:

Minimize the objective function (Obj)

$$Obj = f(\bar{X})$$

Subject to:

Inequality constraints (G)

$$G_j(\bar{X}) \le 0 \qquad j = 1,2,\ldots,m$$

Equality constraints (H)

$$H_j(\bar{X}) = 0 \qquad j = 1,2,\ldots,l$$

Side constraints

$$X_i^l \le X_i \le X_i^u \qquad i = 1,2,\ldots,n$$

Returning to the cantilevered beam problem, it may be
stated in the standard format as follows:

Let $X(1) = B$, $X(2) = H$, and $Obj = Vol = B \cdot H \cdot L$

Then minimize $Obj = Vol$

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Subject to:

$$G(1) = \frac{\sigma_b}{20000} - 1 \leq 0$$

$$G(2) = \frac{\nu}{10000} - 1 \leq 0$$

$$G(3) = \delta - 1 \leq 0$$

$$G(4) = \frac{H}{B} - 10 \leq 0$$

With side constraints:

$$X(1)^l = 0.5$$
$$X(1)^u = 5.0$$
$$X(2)^l = 1.0$$
$$X(2)^u = 20.0$$

It is thus fairly simple and straightforward to perform an analysis on a particular beam for a given B and H. Successive analyses may be performed on the cantilevered beam by solving the above system of equations. It is desirable to automate the successive solutions and to direct the solutions such that each solution is a better design than the last. One approach for doing so, and the one used by DESOP is to proceed as follows: Start with initial values for B and H. Solve the above set of equations to find the objective function Obj and to see if any constraints are violated. A pseudo objective function is created to represent designs when constraints are violated. If a constraint is violated, a penalty is added to Obj to form a penalized objective function Opj. The gradient of the

penalized objective function at the initial design may be found by taking the first partial derivative of Opj with respect to the design variables. The gradient of the penalized objective function defines the direction of steepest ascent. In the case of the cantilevered beam, it is desired to minimize the objective function; therefore, the greatest improvement in design may be achieved by moving in the negative gradient, or steepest descent direction. From the initial design point a search is performed in the steepest descent direction for the minimum value of Opj in that direction. At the new minimum, the gradient of the penalized objective function is again determined and a search is performed in a conjugate direction until a second minimum is found. Successive iterations are performed until the gradient is found to be zero or each successive iteration produces a sufficiently small change in Opj such that for all practical purposes the minimum has been found. At this time the penalty function is increased. If the design is in a region where there are no constraints violated an increase in the penalty function will not change the value of Opj. If on the other hand the design is in an infeasible region where there are one or more constraints violated, Opj will be increased, and the search for a new minimum will commence. If the minimum of the objective function exists in the infeasible region,

the minimum value for the objective function in the feasible region will be approached from the infeasible region as the penalty function is increased. The design improvement process will terminate when a zero gradient is found or successive iterations produce a sufficiently small change in the value of Opj and an increase in the penalty function causes no change in Opj.

The minimum thus reached by the optimization process is a minimum with respect to the penalized objective surface immediately surrounding the final design point. The optimization process cannot distinguish between local and global minimum points. It is thus good engineering practice to run several optimizations for a particular design problem from several different initial design points. If optimizations performed from different initial design points converge on the same minimum point, that point is probably a global minimum. If on the other hand two or more minimums are found, there may be local minimums located in the design space being considered and care must be taken to find the global minimum.

C.   THE DESOP NUMERICAL OPTIMIZATION PROGRAM

The DEsktop Sequential unconstrained minimization technique OptimIzation Program was developed using the basic optimization approach outlined in Section II.A. A copy of the program is included in Appendix E. The major

program structure is shown in Figure 2. The following discussion will refer to Figure 2 and describe the major features of the program.

1. Basic Program Execution

The DESOP program begins execution when it is loaded, linked to the user's analysis subprogram, and the program is instructed to run by the OPCON program. The above actions are automatically performed by the OPCON program. DESOP is loaded into the computer by an overlay process. Therefore no variables can be directly transferred between the DESOP and OPCON programs. DESOP begins execution by reading the optimizer control variables and the design variables that were input using the OPCON program and saved to a mass storage device. The program then sets Icalc equal to one and evaluates the objective function and constraints at the initial design point. Icalc is a flag provided the user to key user specified output on the initial and final design analysis. DESOP will provide the user with a hard copy output of the initial design variables, the value of the constraints, the objective function and the penalized objective function. The user then has the option of continuing with the DESOP program to optimize his analysis subprogram or to return to the OPCON program to change one or more of the input parameters.

Figure 2. DESOP Flow Diagram

Proceeding with the optimization, there are two major loops in the optimization program. The outer loop increases the penalty function when the inner loop's convergence criteria have been met. A convergence test is then performed by the outer loop. If the convergence criteria is met, the optimization process is considered finished. If the convergence criteria for the outer loop is not met, program execution is returned to the inner loop. The inner loop performs successive iterations searching for the minimum of the penalized objective function with no increase in the penalty function taking place. When the inner loop's convergence criteria have been met program execution is transferred to the outer loop.

Execution of the program while in the inner loop proceeds as follows: First, the gradient of the penalized objective function is calculated by subroutine GRAD. The program then computes a search direction using either a steepest descent method or the method of conjugate directions developed by Fletcher and Reeves [Ref. 1]. Once a search direction is established the optimizer attempts to locate the minimum value of the penalized objective function in the search direction. This process if referred to as the one-dimensional search and is illustrated in Figure 3. The efficiency and accuracy to which the one-dimensional search for the minimum of the penalized objective function

Opj

0   6   15.7   21.7 25.4 27.8   31.4   41.4 α

EXPANDING SEARCH FOR THE MINIMUM
αz^1 $\alpha 3^1$
αz^2 $\alpha 1^2$ $\alpha 3^2$
         αz^3 $\alpha 1^3$

MINIMUM BRACKETED - GOLDEN SECTION SEARCH TO LOCALIZE THE MINIMUM
         αz^4 $\alpha 1^4$ $\alpha 2^4$ $\alpha 3^3$
         αz^5 $\alpha 2^5$ $\alpha 3^5$ $\alpha 3^3$

$Opj1^4 < Opj2^4$

$Opj1^5 > Opj2^5$ $\alpha 1^5$
         αz^6 $\alpha 1^6$ $\alpha 2^6$ $\alpha 3^6$

Figure 3.   The One-Dimensional Search Process

is accomplished, is the key to successful sequential un-constrained minimization technique numerical optimization. The one-dimensional problem may be expressed in terms of the penalized objective function, Opj, and the amount of movement, α, in the search direction, $\bar{S}$. First the slope of Opj with respect to α is calculated. An initial "guess" of how far to move is made using subroutine ALPGES. The α which corresponds to the minimum value of Opj in the one-dimensional search is then calculated using subroutine ALPBND and subroutine QUEBIC. The minimum value of Opj thus found is then compared to the previous value of Opj for convergence using subroutine CONVRG. If convergence is not met, execution returns to the start of the inner loop. If convergence is met, execution returns to the outer loop.

When the convergence criteria have been met for both the inner and outer loops, the program proceeds to set ICALC to three as a flag for user generated output for the final design. DESOP then provides the user with a hard copy output of the final design variables, objective function value, penalized objective value, constraint values, the number of inner loop iterations, the number of times the analysis subprogram was called and the final value of the penalty function. The OPCON program is then overlayed over the DESOP program and program execution is returned to the OPCON program.

2. Finding the Search Direction

The first step in finding the search direction, $\bar{S}$, is to determine the slope of Opj at the present design point. The forward finite difference method is used where:

$$\frac{\partial F}{\partial X_i} = \frac{F(X_i + \Delta X_i) - F(X_i)}{\Delta X_i} = -S_i$$

$$i = 1,2,\ldots Ndv$$

As $\partial F/\partial X_i$ gives the direction of positive slope, the search direction is the negative of $\partial F/\partial X_i$. The first search is performed using the steepest descent as found above using the following relation:

$$X_i' = X_i + \alpha S_i$$

where alpha is the distance moved in the $\bar{S}$ direction. When a minimum is obtained along the direction of steepest descent, a new Fletcher-Reeves conjugate search direction [Ref. 1] is calculated at the new Design point using the following relations:

$$S_i' = \frac{\partial F}{\partial X_i} + BS_i$$

$$B = \frac{\sum\limits_{i=1}^{Ndv} [\frac{\partial F'}{\partial X_i}]^2}{\sum\limits_{i=1}^{Ndv} [\frac{\partial F}{X_i}]^2}$$

where the prime denotes values for the present iteration and the non-prime variables indicate values for the previous

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iteration. A one-dimensional search is then performed in the new search direction. Searches are continued using the conjugate direction method for Ndv + 1 iterations, where Ndv is the number of design variables. The search process is then restarted using the steepest descent method. The reason for incorporating the conjugate search method is that the steepest descent method when traversing a design surface with a curved valley will tend to zigzag from one side of the design surface valley to the other making very little progress as is illustrated in Figure 4. The conjugate direction method is much more efficient in traversing such a design surface. However, as the conjugate direction method is additive upon previous searches, it has a tendency to decrease in effectiveness with each successive search owing to the accumulation of numerical "noise." For that reason the search process is restarted with the steepest descent method every Ndv + 1 iterations, or when the conjugate direction predicts a positive slope. The search direction is normalized to avoid inaccuracies caused by numerical ill-conditioning.

3. Estimating an Initial Value for Alpha

The initial estimate for alpha is made in the following manner: First, the slope of Opj in the search direction is calculated as the sum of each of the products of the gradients times the search direction. Then the slope of Opj in the search direction is divided by the value

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Figure 4. Steepest Descent and Conjugate Direction Search in a Two-Dimension Design Space.

of Opj. This value is then multiplied by an improvement
percentage in Opj. This first estimate is then applied to
a series of conditional tests to determine the validity of
the estimate with respect to the slope of Opj and the magni-
tude of the design variables. Lastly, the estimate for
alpha is checkec to see if it violates any side constraints.
If it does, the value of the estimate for alpha is reduced
until the side constraints are no longer violated.

    4. Calculating Alpha

        The calculation of alpha is the most critical al-
gorithm in the DESOP program in providing reliable optimizer
operation. The ability to accurately and efficiently find
the minimum of the penalized objective function in the one-
dimensional search affects directly the operation of the
optimizer. Figure 5 illustrates the zigzag phenomenon
which occurs if alpha is not accurately found. The zigzag
phenomenon is caused by the fact that the optimizer in per-
forming the forward finite difference for calculating the
search direction perturbs the design vector a very small
amount. As such the optimizer can only "see" the design
surface that is immediately adjacent to the design point.
Therefore, if the minimum is not found in the one-dimensional
search, the optimizer will converge very slowly on the
minimum.

        There are tow major sections to the ALPBND subroutine.
The first section attempts to find the minimum value of Opj

Figure 5. The Zigzag Phenomenon

using an expanding search technique. The first move is
the amount predicted by the ALPGES subroutine. If the
minimum is not bracketed by the first move, additional
moves are made. Each move is larger than the last. The
size of the move is increased each time by an amount equal
to the size of the last move divided by the lower Golden
Section fraction, where the Golden Section fractions are:

$$F_1 = \frac{3 - \sqrt{5}}{2}$$

$$F_2 = \frac{\sqrt{5} - 1}{2}$$

The lower Golden Section fraction, F_1, is used so that the
interval will be consistent with the Golden Section search
in the second section of the ALPBND subroutine. The expand-
ing search is continued until the minimum value of the ob-
jective function has been bracketed.

Once the minimum is bracketed, a Golden Section
search is performed to reduce the bracketing interval on
the minimum by an amount such that when the two end points
of the interval are taken with two points internal to the
interval and a cubic is passed through the four points, the
cubic will accurately predict the minimum of the penalized
objective function. Himmelblau in [Ref. 2] states that the
Golden Section search method of reducing the interval
around the minimum of Opj is the most effective of the
reducing techniques studied. Golden Section search is based

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on the splitting of a line into two segments known in ancient times as the "Golden Section." The ratio of the whole line to the larger segment is the same as the ratio of the larger segment to the smaller segment. The two Golden Section fractions are employed to split the interval bracketing the minimum as shown in Figure 3. Once the interval has been split, the two values of Opj corresponding to the internal points are compared to find the larger of the two. The internal point with the larger value of Opj will become the new end point for the interval, the remaining interior point will by the fact that it was determined by a Golden Section fraction, be equal to the point determined by the other Golden Section fraction. Thus, only one new point must be calculated to continue the Golden Section search. The search is continued in this manner until the vertical separation of the two end points with respect to the interior points is less than one percent. The four values of the penalized objective function corresponding to the four Golden Section search points are then sent to a cubic interpolator. The cubic interpolator will return a value for alpha to predict the minimum of the penalized objective function, and the minimum of the cubic function that the interpolator has created. The subroutine ALPBND will then test the predicted minimum with the minimum found at the predicted alpha. If there is less than a tenth of

one percent difference between the two values of the objective function, the point predicted by the cubic interpolator will be accepted as the minimum and program execution will return to the main program. If the predicted minimum is not sufficiently close to the minimum at the predicted alpha, another Golden Section search will be performed to reduce the interval and better localize the minimum. The four points from the reduced interval will then be sent to the cubic interpolation subroutine. This process will continue until either the test for the minimum is positive or the interval has been reduced to less than 1E-12. Program execution will then return to the main program.

5. Subroutine QUEBIC

Subroutine QUEBIC is used to estimate the alpha at which Opj is a minimum based on four point cubic interpolation. If the function more closely resembles a quadratic than a cubic, a three point quadratic interpolation is performed using the three points which bracket the minimum. If the predicted minimum is outside the interval spanned by the two end points again a quadratic interpolation is performed. If the minimum still lies outside the two end points, the analysis returns to subroutine ALPBND, the inverval bracketing the minimum is reduced, and program execution returns to QUEBIC.

6. Convergence of the Penalized Objective Function

The penalized objective function is tested for convergence at the end of each inner loop and again at the end of the outer loop in the main program. Convergence is tested by calling subroutine CONVRG. There are two criteria used for testing for convergence. The first tests the relative difference of the value of Opj from the present iteration with the value of Opj from the last iteration. The second method tests the absolute difference of the two values. The second method is employed for cases when the value of the penalized objective function approaches zero. When convergence has been met on two successive iterations, the penalty function is increased by an amount specified by the user in the executive OPCON program. The penalized objective function is again tested for convergence. If convergence is still met, the optimizer considers the present value of the penalized objective function to be a minimum, noting again that numerical optimization programs cannot differentiate between local and global minimums.

7. The Penalty Function

The purpose of the penalty function is to increase the value of the objective function when the design is in an infeasible region. The infeasible region is that region where one or more design constraints are violated. When a constraint is violated, the value of the particular constraint,

G_j, is positive. The objective function is then penalized
as follows:

$$Opj = Obj + R \cdot G_j E$$

where:

R - a multiplication constant

E - an exponent constant

This type of penalty function, one where the penalty is
applied after the design leaves the feasible region, is
known as an exterior penalty function. The exterior type
of penalty function was chosen over other types, such as
the interior or extended interior penalty function. If a
function is discontinuous within the design space being
studied, numerical difficulties may be encountered which
make performing an optimization of the design difficult.

D. USE OF THE DESOP NUMERICAL OPTIMIZATION PROGRAM

Once the analysis subprogram has been written and SAVED, the user may perform a numerical optimization of the design analysis. Figure 11 shows the basic relationships between the OPCON and DESOP programs and the user supplied ANALIZ subprograms. Note that the DESOP program overlays the OPCON program after all data has been input. To begin, LOAD OPCON and press run. Through a series of self-explanatory menus, the user will be prompted to input control variables, design variables and execute the DESOP program. The following menus appear in the OPCON program.

1. INTRODUCTION - A brief introduction stating the purpose of the OPCON program.

2. NEW OR EXISTING ANALYSIS PROGRAM - If this is the first time that a particular analysis subprogram has been run on the tape or disk being used, or if the files from a subsequent run have been deleted, the user must enter the response for a new analysis subprogram. For existing programs, OPCON will read data from the existing data file. The data read will be that from the subsequent run of the particular analysis subprogram.

3. NAME THE ANALIZ SUBPROGRAM - The user will input the name under which the analysis subprogram he wishes to use was saved. If this is a new analysis subprogram OPCON will create files for saving the data input during the execution of OPCON.

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4. OPTIMIZER SELECTION - At the present time there is only one optimization program available. It is hoped that at some future date additional numerical optimization programs will be added to the optimization package. OPCON has been developed to interface with multiple numerical optimization programs. Details for linking other numerical optimization programs to OPCON are included as comments in the OPCON listing which may be found in Appendix D.

5. INPUT NDV AND NCON - For a new analysis subprogram the user will be asked to input the number of design variables, NDV, and the number of constraints in the analysis subprogram, NCON.

6. INPUT CHECK OF COMMON CONTROL VARIABLES - A menu of the optimizer control parameters common to DESOP, Feasible Direction type and other future optimization programs is displayed. The menu displays the variable name, its minimum, maximum, default and present value. The variables displayed are:

NDV - The number of independent design variables used in the analysis code.

NCON - The number of constraints in the design analysis subprogram.

IPRINT - A print control used in the optimization program to display intermediate results. Positive values entered will print on the CRT. Negative values entered

will print on the thermal printer. If a zero is entered there will not be a hard copy output of the initial and final results of the optimization program. IPRINT = 0 is to be used when debugging an analysis subprogram to conserve thermal paper.

+1 - Print initial and final optimization information.

+2 - Print above plus the objective function and penalized objective function on each iteration.

+3 - Print above plus the constraint values, search direction vector and move parameter alpha on each iteration.

+4 - Print above plus gradient information on each iteration.

+5 - Print above plus each proposed design vector and the penalized objective function during the one-dimensional search on each iteration.

+6 - Debugging aid for optimizer development. DESOP will pause after each major operation is performed during the optimization process.

DELFUN - The minimum absolute change in the objective function to indicate convergence of the optimization process.

DABFUN - The minimum absolute change in the objective function to indicate convergence of the optimization process.

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ITMAX - The maximum number of inner loop (unconstrained minimizations) without increasing the penalty function.

ICNDIR - The conjugate direction restart parameter. Every ICNDIR inner loop iterations a steepest descent search is performed. It is recommended that ICNDIR be set equal to NDV + 1.

FDCH - The relative change in the design variables for calculating finite difference gradients.

FDCHM - The minimum absolute step in finite difference gradient calculations.

ABOBJ1 - The expected fractional change in the objective function for the first estimates of the step size to be taken in the one-dimensional search.

ALPHAX - The maximum fractional change in any design variable for the first estimate of the step size to be taken in the one-dimensional search.

7. INPUT CHECK OF THE DESOP CONTROL PARAMETERS - A menu of the optimizer control parameters for the DESOP optimization program is displayed. The menu will display the variable name, its maximum, minimum, default and present value. The variables displayed are:

IRMAX - The maximum number of times that the penalty parameter will be increased.

RZ - The starting value of the penalty parameter.

RMULT - The amount by which RZ is multiplied each time that it is increased.

EXPG - The amount by which a violated constraint value is raised to an exponent, EXPG.

NSCAL - A design variable auto-scaling control.

0 - No scaling of the design variables is performed by DESOP.

1 - The design variables are scaled every ICNDIR iteration.

9. INPUT DESIGN VARIABLES AND SIDE CONSTRAINTS - A menu of the initial design variables and constraints will be displayed for an existing analysis subprogram. If this is a new analysis subprogram, the user will be asked to enter the initial values of the design variables and any side constraints on the design variables.

A hard copy printout of the optimizer control parameters, design variables and side constraints will then be presented to the user to check to ensure that the above information has been entered correctly. The user then has the option to return to the input routine and make changes to the above information or to continue and optimize his design. If the user chooses to continue, OPCON will overlay the optimization program on OPCON beginning at line C2. The analyze subprogram specified will then be linked to the end of the DESOP program. The entire program will then be STORED under the program name OP. The OP program will then be loaded with

execution beginning at line OPT1. The storing and reloading process allows the OP program to be called and run as a separate program for debugging purposes. At the completion of the optimization process, the optimizer program will reload OPCON and return execution to the OPCON program. A menu will be displayed welcoming the user back to the OPCON program giving him the following options: to optimize again using the same ANALIZ subprogram, to optimize again using a different ANALIZ subprogram, or to terminate the program.

APPENDIX D

OPCON Program Listing

```
100 ! *************************************************************
110 ! *                                                           *
120 ! *                        OPCON                              *
130 ! *                                                           *
140 ! *   THE EXECUTIVE PROGRAM FOR PERFORMING NUMERICAL          *
150 ! *   OPTIMIZATION ON THE HP 9845A COMPUTER                   *
160 ! *                                                           *
170 ! *              by W. B. COLE                                *
180 ! *   NAVAL POSTGRADUATE SCHOOL, MONTEREY, CALIFORNIA         *
190 ! *              1980                                         *
200 ! *                                                           *
210 ! *************************************************************
220 !
230 !
240 ! FUNCTIONS :
250 !    1.  INPUT AND STORAGE OF CONTROL PARAMETERS FOR THE OPTIMIZERS USED
260 !    2.  INPUT AND STORAGE OF THE DESIGN VARIABLES AND SIDE CONSTRAINTS
270 !        ON THE OPTIMIZERS USED
280 !    3.  CONTROL OF THE OPTIMIZATION PROCESS THROUGH THE USE OF OVERLAYS
290 ! ---------------------------------------------------------------
300 ! ---------------------------------------------------------------
310 ! NOTE: OPCON was written to control multiple optimization programs.  At
320 !       the present time DESOP is the only optimizer working.  A Feasible
330 !       Directions optimizer has been partialy written and debugged.  At
340 !       the present time OPCON has been written to accept the control
350 !       parameters for the Feasible Direction optimization program.
360 ! ---------------------------------------------------------------
370 ! ------- CONTROL SECTION ------
380 ! ---------------------------------------------------------------
390 COM Globcm(50),F$,D$,Analiz$
400 GOTO C7
```

```
410  !-------------------------------------------------------------------
420  C1:  !          ----- CONTROL FOR SUMT OPTIMIZER -----
430  !-------------------------------------------------------------------
440  PRINTER IS 16
450  PRINT PAGE
460  PRINT LIN(5),TAB(10)," LINKING SUMT OPTIMIZER AND ";Analiz$;" ROUTINE."
470  LINK Opt,C2
480  LINK Analiz$,Analiz1
490  RE-STORE "OP"
500  LOAD "OP",Opt1
510  !-------------------------------------------------------------------
520  C2:  !          ----- ATTACHMENT POINT FOR OPTIMIZER -----
530  !-------------------------------------------------------------------
540  !-------------------------------------------------------------------
550  !-------------------------------------------------------------------
560  C7:  !          ----- INTRODUCTION -----
570  !-------------------------------------------------------------------
580  PRINTER IS 16
590  PRINT PAGE
600  PRINT "
610  PRINT LIN(2),"OPCON          ***    OPCON    ***"
IZATION ON "
620  PRINT LIN(1),"THE HP 9845 DESKTOP COMPUTER."
630  PRINT LIN(2),"THE FUNCTIONS OF OPCON ARE :"
640  PRINT LIN(1),"      1.   THE INPUT AND STORAGE OF CONTROL PARAMETERS.
"
650  PRINT "      2.   THE INPUT AND STORAGE OF DESIGN VARIABLES."
660  PRINT "      3.   CONTROL OF THE OPTIMIZATION PROCESS THROUGH PROGRAM
OVERLAYS."
670  DISP " PRESS 'CONT' "
680  PAUSE
690  GOTO C10
```

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```
700 ' -------------------------------------------
710 C8: '
720 ' ----- RETURN FROM OPTIMIZATION -----
730 PRINTER IS 16
740 PRINT PAGE
750 PRINT "          *** WELCOME BACK *** "
760 PRINT LIN(1),"WELCOME BACK TO 'OPCON'.   YOU NOW HAVE SEVERAL AVAILABLE OPT
IONS."
770 PRINT LIN(1),"        1.   OPTIMIZE THE ";Analiz$;" FUNCTION."
780 PRINT LIN(1),"        2.   OPTIMIZE A DIFFERENT ANALIZE FUNCTION."
790 PRINT LIN(1),"        3.   TERMINATE THE PROGRAM."
800 INPUT " INPUT YOUR CHOICE : 1,2 OR 3 .",Ch
810 IF Ch=1 THEN Prog1=1
820 IF Ch=1 THEN GOTO C13
830 IF Ch=2 THEN Prog1=0
840 IF Ch=2 THEN GOTO C12
850 IF Ch=3 THEN PRINT PAGE
860 IF Ch=3 THEN PRINT "                         END OF PROGRAM"
870 IF Ch=3 THEN GOTO 299
880 GOSUB Err
890 GOTO C8
900 ' -------------------------------------------
910 C9: '
920 ' ----- RETURN FROM END OF INPUT ROUTINE -----
930 PRINTER IS 16
940 PRINT PAGE
950 PRINT "DO YOU STILL WISH TO OPTIMIZE THE ";Analiz$;" FUNCTION?"
960 INPUT " ( 1 - YES : 0 - NO )",Ch
970 IF Ch=0 THEN C10
980 IF Ch=1 THEN Para9
990 GOSUB Err
1000 GOTO C9
```

101

```
1010 ! ----------------------------------------------------------

1020 C10:  !              ----- CONTROL PARAMETER INPUT -----
1030 ! ----------------------------------------------------------
!
1040 DIM Lmin(4),Ladd(4),P(50,4),Param$(50),X(30),V1b(30),Vub(30)
1050 DIM S$(40),Params(50)
1060 PRINTER IS 16 ! (CRT)
1070 PRINT PAGE
1080 ! ----------------------------------------------------------
!
1090 C11:  !            ----- NEW OR EXISTING PROGRAM ? -----
1100 ! ----------------------------------------------------------
1110 PRINT LIN(3),TAB(17),"IS THIS A NEW OR EXISTING PROGRAM ?"
1120 INPUT "   INPUT : ( NEW = 0 , EXISTING = 1 ) ",Prog1
1130 ! ----------------------------------------------------------
1140 C12:  !            ----- NAME THE ANALIZE PROGRAM -----
1150 ! ----------------------------------------------------------
1160 PRINT PAGE
1170 PRINT LIN(3),TAB(10),"WHAT IS THE NAME OF THE ANALIZE PROGRAM ?"
1180 INPUT "   INPUT THE NAME : ",Analiz$
1190 DISP "CREATING NEW FILES FOR ";Analiz$
1200 P$="P"                         ! ASSIGN PARAMETER AND DESIGN VARIABLE
1210 D$="D"                         ! FILE NAMES TO MATCH THE ANALIZE
1220 P$[2,6]=Analiz$                ! ROUTINE.
1230 D$[2,6]=Analiz$
1240 IF Prog1=1 THEN GOTO 1290      ! IF THIS IS A NEW PROGRAM, CREATE THE
1250 ON ERROR GOTO Err1
1260 CREATE P$,4
1270 CREATE D$,3
1280 OFF ERROR
1290 PRINT PAGE
```

```
1300 ! --------------------------------------------
1310 C13: !              ----- OPTIMIZER SELECTION -----
1320 ! --------------------------------------------
1330 PRINT LIN(3),TAB(5),"WHICH OF THE FOLLOWING OPTIMIZERS DO YOU WISH TO US
E ?"
1340 PRINT LIN(1),TAB(5),"1.  SEQUENTIAL UNCONSTRAINED OPTIMIZATION.  DESOP"
1350 ! PRINT LIN(1),TAB(5),"2.  FEASIBLE-DIRECTION OPTIMIZATION."
1360 PRINT LIN(3)," AT THE PRESENT TIME DESOP IS THE ONLY OPTIMIZATION PROG
RAM AVAILABLE."
1370 INPUT " INPUT THE OPTIMIZER NUMBER : ",Prog2
1380 IF Prog2=1 THEN Opt$="DESOP"
1390 IF Prog2=2 THEN Opt$="OPT-2"
1400 IF Prog1=1 THEN GOTO Para10
1410 ! --------------------------------------------
1420 C14: !        ----- INPUT INITIAL VALUE FOR NDV -----
1430 ! --------------------------------------------
1440 Param$(1)="NDV"
1450 P(1,1)=1
1460 P(1,2)=30
1470 P(1,3)=0
1480 PRINT PAGE
1490 PRINT LIN(3),TAB(5)," INPUT THE NUMBER OF DESIGN VARIABLES ( NDV )  "
1500 PRINT TAB(5),"MIN = ",P(1,1)
1510 PRINT TAB(5),"MAX = ",P(1,2)
1520 INPUT " Ndv = ? ",P(1,4)
1530 Ndv=P(1,4)
1540 IF (P(1,4)>=P(1,1)) AND (P(1,4)<=P(1,2)) THEN Para10
1550 GOSUB Err
1560 GOTO 1480
1570 Para10: ! CONTINUE
```

103

```
1580  !------------------------------------------
1590  !----- CONTROL PARAMETER DATA -----
1600  !------------------------------------------
1610  DATA 2,10
1620  DATA NCON,0,20,0
1630  DATA IPRINT,-5,6,0
1640  DATA DELFUN,0.0,0.1,0.001
1650  DATA DABFUN,0.0,0.1,0.001
1660  DATA ITMAX,1,100,20
1670  DATA ICHDIR,2,21,5
1680  DATA FDCH,1E-5 ,0.1,0.001
1690  DATA FDCHM,1E-6 ,0.1,0.0001
1700  DATA ABOBJ1,0.01,0.5,0.1
1710  DATA ALPHAX,0.01,0.5,0.1
1720  !------------------------------------------
1730  !----- OPTIMIZER #2 CONTROL PARAMETERS -----
1740  !------------------------------------------
1750  DATA 20,10
1760  DATA IPDEG,0,1,0
1770  DATA CT,0,1,0.1
1780  DATA CTMIN,-0.01,0,-0.004
1790  DATA CTL,0,1,0.1
1800  DATA CTLMIN,-0.1,0,-0.001
1810  DATA PHI,1,100,5
1820  DATA THETA,0,10,1
1830  DATA ITRM,1,5,3
1840  DATA CG,0,1,0
1850  DATA NCF,0,40,0
```

```
1860  !-------------------------------------------------------------------
1870  !             ----- OPTIMIZER #1 CONTROL PARAMETERS -----
1880  !-------------------------------------------------------------------
1890  DATA 40,5
1900  DATA IRMAX,1,30,10              ! MAXIMUM NUMBER OF PENALTY ITERATIONS
1910  DATA RZ,.0001,9999,2            ! INITIAL PENALTY FUNCTION
1920  DATA RMULT,0.001,1000,2         ! PENALTY FUNCTION MULTIPLIER
1930  DATA EXPG,1,10,2                ! PENALTY FUNCTION EXPONENT
1940  DATA NSCAL,0,1,1                ! DESIGN VARIABLE SCALING 1-YES 0-NO
1950  FOR K=1 TO 3                    ! READ DATA
1960  READ Lmin(K),Ladd(K)
1970  FOR I=Lmin(K) TO Lmin(K)+Ladd(K)-1
1980  READ Param$(I),P(I,1),P(I,2),P(I,3)
1990  NEXT I
2000  NEXT K
2010  IF Prog1=1 THEN GOTO P3         ! (CONTINUE)
2020  FOR I=2 TO 50
2030  P(I,4)=P(I,3)
2040  NEXT I
2050  !-------------------------------------------------------------------
2060  P3:      !     ----- IF EXISTING PROGRAM - READ EXISTING VALUES -----
2070  !-------------------------------------------------------------------
2080  IF Prog1=0 THEN Para9           ! IF NOT CONTINUE
2090  Param$(1)="NDV"
2100  DISP "READING EXISTING CONTROL PARAMETERS AND DESIGN VARIABLES."
2110  ASSIGN #1 TO P$
2120  ASSIGN #2 TO D$
2130  FOR J=1 TO 3
2140  READ #1,J
2150  K=Lmin(J)-(J=1)
2160  K1=K+Ladd(J)-1+(J=1)
2170  FOR I=K TO K1
2180  READ #1;P(I,4)
2190  NEXT I
2200  NEXT J
2210  Ndv=P(1,4)
```

105

```
2220 !----------------------------------------
2230 !          ------ READ EXISTING DESIGN VARIABLES ------
2240 !----------------------------------------
2250 READ #2,1
2260 FOR I=1 TO Ndv
2270 READ #2;X(I)
2280 NEXT I
2290 READ #2,2
2300 FOR I=1 TO Ndv
2310 READ #2;Vlb(I),Vub(I)
2320 NEXT I
2330 Para9: ! CONTINUE
2340 !----------------------------------------
2350 !          ------ INPUT CHECK ------
2360 !----------------------------------------
2370 K=1
2380 PRINT PAGE
2390 PRINT TAB(10),"INPUT CHECK OF COMMON CONTROL PARAMETERS"
2400 PRINT LIN(1)
2410 PRINT "REF #   PARAMETER      MINIMUM      MAXIMUM    RECOMMENDED
PRESENT"
2420 IMAGE 4X,"1",3X,6A,4X,M4D.4D,4X,M4D.4D,8X,"*****",4X,M4D.4D
2430 PRINT USING 2420;Param$(1),P(1,1),P(1,2),P(1,4)
2440 IMAGE 4X,"2",3X,6A,4X,M4D.4D,4X,M4D.4D,8X,"*****",4X,M4D.4D
2450 PRINT USING 2440;Param$(2),P(2,1),P(2,2),P(2,4)
2460 FOR I=3 TO Ladd(1)+1
2470 IMAGE 3X,DD,3X,6A,4(4X,M4D.4D)
2480 PRINT USING 2470;I,Param$(I),P(I,1),P(I,2),P(I,3),P(I,4)
2490 NEXT I
2500 PRINT LIN(1)," NOTE : IFRINT = 6 IS DEBUG MODE, THERE IS NO HARDCOPY OU
TPUT."
2510 IF Ie=1 THEN GOTO 2560
2520 INPUT "DO YOU WISH TO MAKE ANY CHANGES?  ENTER REF# OR 0 FOR NONE.",Ch
2530 IF Ch=0 THEN Parall
2540 IF (Ch<0) OR (Ch>Ladd(K)+1) THEN GOSUB Err
2550 IF (Ch<0) OR (Ch>Ladd(K)+1) THEN GOTO 2380
```

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```
2560    DISP "INPUT THE CHANGE TO ";Param$(Ch);
2570    INPUT Pch
2580    IF (Pch>=P(Ch,1)) AND (Pch<=P(Ch,2)) THEN Para13
2590    GOSUB Err
2600    Ie=1
2610    GOTO 2380
2620    Para13:  P(Ch,4)=Pch
2630    Ie=0
2640    GOTO 2380
2650    Para12: ! ( INPUT ERROR )
2660    GOTO 2380
2670    !------------------------------------------------------------
2680    Para11: !  ----- INPUT CHECK  FEASIBLE-DIRECTION -----
2690    !------------------------------------------------------------
2700    GOTO Para15                    ! LOOP AROUND FEASIBLE DIRECTION
2710    PRINT PAGE
2720    IF Prog2<>1 THEN Para15
2730    K=2
2740    PRINT TAB(5);"INPUT CHECK   -   USABLE-FEASIBLE CONTROL PARAMETERS"
2750    PRINT LIN(1)
2760    PRINT "REF #   PARAMETER    MINIMUM      MAXIMUM    RECOMMENDED
        PRESENT"
2770    FOR I=Lmin(K) TO Lmin(K)+Ladd(K)
2780    IMAGE 3X,DD,3X,6A,4(4X,M4D.4D)
2790    PRINT USING 2780;I,Param$(I),P(I,1),P(I,2),P(I,3),P(I,4)
2800    NEXT I
2810    IF Ie=1 THEN Para14
2820    PRINT LIN(2),"DO YOU WISH TO MAKE ANY CHANGES ?"
2830    INPUT " ( INPUT : REF #  -OR-  0  FOR NONE )",Ch
2840    IF Ch=0 THEN Para15
2850    IF (Ch<Lmin(K)) OR (Ch>Lmin(K)+Ladd(K)) THEN GOSUB Err
2860    IF (Ch<Lmin(K)) OR (Ch>Lmin(K)+Ladd(K)) THEN GOTO 2710
2870    Para14:  DISP "INPUT THE CHANGE TO ";Param$(Ch);
2880    INPUT Pch
2895    IF (Pch>=P(Ch,1)) AND (Pch<=P(Ch,2)) THEN Para17
2900    GOSUB Err
2910    Ie=1
```

```
2920    GOTO 2710
2930    Para17: P(Ch,4)=Fch
2940    Ie=0
2950    GOTO 2710
2960    !-------------------------------------------------------------
2970    Para15: !        ----- INPUT CHECK DESOP -----
2980    !-------------------------------------------------------------
2990    PRINT PAGE
3000    IF Prog2<>2 THEN Para25
3010    K=3
3020    PRINT TAB(15),"INPUT CHECK  -  'SUM' CONTROL PARAMETERS"
3030    PRINT LIN(1)
3040    PRINT "REF #   PARAMETER    MINIMUM      MAXIMUM      RECOMMENDED
PRESENT"
3050    FOR I=Lmin(K) TO Lmin(K)+Ladd(K)-1
3060    IMAGE 3X,DD,3X,6A,4(4X,M4D.4D)
3070    PRINT USING 2780;I,Param$(I),P(I,1),P(I,2),P(I,3),P(I,4)
3080    NEXT I
3090    IF Ie=1 THEN Para14
3100    PRINT LIN(2),"DO YOU WISH TO MAKE ANY CHANGES ?"
3110    INPUT " ( INPUT : REF #  -OR-  0  FOR NONE )",Ch
3120    IF Ch=0 THEN Para25
3130    IF (Ch<Lmin(K)) OR (Ch>Lmin(K)+Ladd(K)) THEN GOSUB Err
3140    IF (Ch<Lmin(K)) OR (Ch>Lmin(K)+Ladd(K)) THEN GOTO 2990
3150    Para24:  PRINT LIN(1),"INPUT THE CHANGE TO ";Param$(Ch)
3160    INPUT Pch
3170    IF (Pch>=P(Ch,1)) AND (Pch<=P(Ch,2)) THEN Para27
3180    Ie=1
3190    GOTO 2990
3200    Para27: P(Ch,4)=Fch
3210    Ie=0
3220    GOTO 2990
3230    Para25: ! CONTINUE
3240    IF Prog1=1 THEN Sideins        !EXISTING PROGRAM GOTO INPUT CHECK
3250    I1=0
```

```
3260    PRINT PAGE
3270    PRINT TAB(15),"INPUT THE INITIAL VALUES FOR THE DESIGN VARIABLES"
3280    PRINT LIN(1)
3290    GOSUB Sidein
3300    PRINT PAGE
3310    PRINT "END OF INPUT ROUTINE"
3320    !
3330 Sav:  !              ------ SAVE INPUTS ------
3340    !  --------------------------------------
3350    PRINT PAGE
3360    Iprint=P(3,4)
3370    IF Iprint=6 THEN S1
3380    PRINTER IS 0
3390    PRINT LIN(3)
3400    PRINT "-----------------------------------
        ----"
3410    PRINT LIN(3)
3420    PRINT "ANALIZE PROGRAM :  ";Analiz$
3430    IF Prog2=1 THEN PRINT LIN(2),"OPTIMIZER USED :        DESOP"
3440    !  IF Prog2=2 THEN PRINT LIN(2),"OPTIMIZER USED :       FEASIBLE-DIRECTION
3450    PRINT LIN(2),"INPUT FOR OPTIMIZATION :"
3460    PRINT LIN(1)
3470 S1:    DISP "SAVING INPUT PARAMETERS."
3480    ASSIGN #1 TO P$
3490    ASSIGN #2 TO D$               !PUT PARAMS INTO MASS STORAGE
3500    PRINT #1,4;Ladd(1)+1,Ladd(2),Ladd(3)
3510    FOR J=1 TO 3
3520    READ #1,J                     ! J = 1 COMMON CONTROL PARAMS
3530    K=Lmin(J)-(J=1)               ! J = 2 U/F CONTROL PARAMETERS
3540    K1=K+Ladd(J)-1+(J=1)          ! J = 3 SUMT CONTROL PARAMS
3550    FOR I=K TO K1
3560    PRINT Param$(I);"=";P(I,4),
3570    PRINT #1;P(I,4)
3580    NEXT I
3590    PRINT #1;END
3600    NEXT J
```

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```
3610 !------------------------------------------------
3620 !-----        SAVE THE DESIGN VARIABLES     -----
3630 !------------------------------------------------
3640 DISP "SAVING DESIGN VARIABLES"
3650 PRINT LIN(1)
3660 READ #2,1
3670 FOR I=1 TO Ndv
3680 PRINT "X(";I;") = ";X(I),
3690 PRINT #2;X(I)
3700 NEXT I
3710 PRINT #2;END
3720 READ #2,2
3730 PRINT LIN(1)
3740 FOR I=1 TO Ndv                  ! SAVE UPPER AND LOWER BOUNDS
3750 PRINT "VLB("&VAL$(I)&") = ";Vlb(I);TAB(40),"VUB("&VAL$(I)&") = ";Vub(I)
3760 PRINT #2;Vlb(I),Vub(I)
3770 NEXT I
3780 PRINT #2;END
3790 DISP "CHECK YOUR INPUT  -  PRESS 'CONT' TO CONTINUE."
3800 BEEP
3810 PAUSE
3820 GOTO P26
3830 !
3840 Sidein: !------------------------------------------------
3850 !-----        DESIGN VARIABLE INPUT         -----
3860 Addcon=0
3870 FOR I=1 TO Ndv
3880 GOSUB Sidein1
3890 NEXT I
3900 I=0
3910 Sidein2: INPUT "DO YOU WISH TO MAKLE ANY CORRECTIONS? ( 0 FOR NO ; VAR# FOR YES )",I
3920 IF I=0 THEN Sidein3
3930 IF (I>0) AND (I<=P(1,4)) THEN GOSUB Sidein1
3940 IF (I>0) AND (I<=P(1,4)) THEN GOTO Sidein2
3950 GOSUB Err
3960 GOTO Sidein2
```

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```
3970 ! ----------------------------------------
3980 Sideinl: !         ----- INPUT INITIAL DESIGN VARIABLES -----
3990 ! ----------------------------------------
4000 DISP "INPUT INITIAL X("&VAL$(I)&"),VLB,VUB : ( USE N FOR NO LOWER OR UPPE
R BOUND )";
4010   INPUT X(I),L$,U$
4020   IF L$="N" THEN Vlb(I)=-1E50
4030   IF L$<>"N" THEN Vlb(I)=VAL(L$)
4040   IF L$="N" THEN L$="NONE"
4050   IF U$="N" THEN Vub(I)=1E50
4060   IF U$<>"N" THEN Vub(I)=VAL(U$)
4070   IF U$="N" THEN U$="NONE"
4080   PRINT " X("&VAL$(I)&")=";X(I)," VLB=";L$," VUB=";U$
4090   RETURN
4100 Sideln3: J=Ncon+1
4110   FOR I=1 TO P(1,4)
4120   IF Vlb(I)<=-1E49 THEN Sideln4
4130   Wlincon(J)=-I
4140   J=J+1
4150   Addcon=Addcon+1
4160 Sideln4:NEXT I
4170   FOR I=1 TO P(1,4)
4180   IF Vub(I)>=1E49 THEN Sideln5
4190   Wlincon(J)=I
4200   J=J+1
4210   Addcon=Addcon+1
4220 Sideln5:NEXT I
4230   RETURN
```

111

```
4240  ! -----------------------------------------------------------------
4250  Sidein6: !           ----- INPUT CHECK FOR EXISTING PROGRAM -----
4260  ! -----------------------------------------------------------------
4270  PRINT PAGE
4280  PRINT TAB(10),"INPUT CHECK  -  INITIAL VALUES FOR THE DESIGN VARIABLES"
4290  PRINT LIN(2)
4300  Z=Ndv
4310  IF Z>15 THEN Z=15
4320  FOR I=1 TO Z
4330  L$=VAL$(Vlb(I))
4340  IF Vlb(I)=-1E50 THEN L$="NONE"
4350  U$=VAL$(Vub(I))
4360  IF Vub(I)=1E50 THEN U$="NONE"
4370  PRINT I;"  X("&VAL$(I)&")  = ";X(I),"VLB("&VAL$(I)&")  = ";L$,"VUB("&VAL$(
I)&")  = ";U$
4380  NEXT I
4390  DISP "DO YOU WISH TO MAKE ANY CHANGES ( REF# OR 0 FOR NONE ) ";
4400  INPUT Ch
4410  IF Ch=0 THEN Sidein8
4420  IF (Ch>0) AND (Ch<=Z) THEN GOSUB Sidein7
4430  IF (Ch>0) AND (Ch<=Z) THEN Sidein6
4440  GOSUB Err
4450  GOTO Sidein6                   ! TRY AGAIN
```

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```
4460  ! -----------------------------------------------------------------
4470  Sidein7: !          ----- ENTER CHANGE TO DESIGN VARIABLE -----
4480  ! -----------------------------------------------------------------
4490  DISP "INPUT CHANGE TO X("&VAL#(Ch)&"),VLB("&VAL#(Ch)&"),VUB("&VAL#(Ch)&")
      ";
4500  INPUT X(Ch),L#,U#
4510  IF L#="N" THEN Vlb(Ch)=-1E50     ! SET UPPER AND LOWER LIMITS TO
4520  IF U#="N" THEN Vub(Ch)=1E50      ! ±1E99 IF NOT SPECIFIED
4530  IF L#<>"N" THEN Vlb(Ch)=VAL(L#)
4540  IF U#<>"N" THEN Vub(Ch)=VAL(U#)
4550  RETURN                           ! RETURN TO ENTER CHANGES
4560  Sidein8: ! CONTINUE WITH INPUT CHECK
4570  IF Z<=15 THEN Sav
4580  Z=16
4590  PRINT PAGE
4600  PRINT TAB(10),"INPUT CHECK CONT.  -  INITIAL VALUES FOR THE DESIGN VARIA
      BLES"
4610  PRINT LIN(2)
4620  FOR I=2 TO Ndv
4630  PRINT I;"  X("&VAL#(I)&") = ";X(I),"VLB("&VAL#(I)&") = ";Vlb(I),"VUB("&V
      AL#(I)&") = ";Vub(I)
4640  NEXT I
4650  DISP "(DO YOU WISH TO MAKE ANY CHANGES ( REF# OR 0 FOR NONE ) )";
4660  INPUT Ch
4670  IF Ch=0 THEN Sav
4680  IF (Ch>16) AND (Ch<=Ndv) THEN GOSUB Sidein7     ! GOTO PRINT INPUT ROUTINE
4690  IF (Ch>16) AND (Ch<=Ndv) THEN GOTO 4650
4700  GOSUB Err
4710  GOTO 4650
4720  ! -----------------------------------------------------------------
4730  Err: !          ----- ERROR ROUTINE FOR ILLEGAL ENTRY -----
4740  ! -----------------------------------------------------------------
4750  PRINT PAGE
4760  BEEP
4770  PRINT LIN(10),TAB(10),"***** INPUT OUT OF RANGE  -  TRY AGAIN *****"
4780  WAIT 2000
4790  RETURN
```

```
4800  ! ----------------------------------------- ERROR ROUTINE FOR EXISTING PROGRAM -----
4810  Err1:  ! -----------------------------------------
4820  ! -----------------------------------------
4830  PRINTER IS 16
4840  PRINT PAGE
4850  BEEP
4860  PRINT LIN(10),TAB(20),"***** ";Analiz$;" IS AN EXISTING PROGRAM *****"
4870  WAIT 5000
4880  OFF ERROR
4890  GOTO C10
4900  ! -----------------------------------------
4910  Err2:  ! -----------------------------------------
4920  ! -----------------------------------------  ERROR ROUTINE FOR EXISTING DATA -----
4930  PRINT PAGE
4940  BEEP
4950  PRINT TAB(15),"*** READ ERROR ON EXISTING PROGRAM ***"
4960  PRINT LIN(2)
4970  PRINT "A READ ERROR HAS OCCURED WHILE ATTEMPTING TO READ EXISTING DATA."
4980  PRINT "THERE ARE SEVERAL POSSIBLE CAUSES FOR THIS TO HAVE HAPPENED."
4990  PRINT LIN(1),"    1.  A MISTAKE WAS MADE WHILE INPUTING DATA.  IF SO RES
TART"
5000  PRINT "    THE PROGRAM BY PRESSING THE RUN KEY.  "
5010  PRINT LIN(1),"    2.  THE DATA FILES NO LONGER EXIST FOR ";Analiz$;" OR
 HAVE AN ERROR "
5020  PRINT "    IN THEM.  IF THIS IS THE CASE THEY MUST BE ERASED AND THE PR
OGRAM "
5030  PRINT "    RESTARTED AS A NEW PROGRAM.  PRESS THE CONT KEY TO ERASE THE
 EXISTING"
5040  PRINT "    DATA FILES FOR ";Analiz$;" AND RESTART THE PROBLEM."
5050  PAUSE
5060  PURGE P$
5070  PURGE D$
5080  OFF ERROR
5090  GOTO C10
```

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```
5100  ! --------------------------------------------------------
5110  P20: !                        ----- LAST CHANCE -----
5120  !  ----------------------------------------------------
5130  PRINTER IS 16
5140  PRINT PAGE
5150  PRINT TAB(10),"LAST CHANCE TO CHANGE YOUR MIND BEFORE OPTIMIZING"
5160  PRINT LIN(2),TAB(5),"1.  RETURN TO THE CONTROL PARAMETER AND DESIGN VARIA
BLE INPUT ROUTINE."
5170  PRINT LIN(2),TAB(5),"2.  PROCEDE TO OPTIMIZE THE ";Analiz$;" FUNCTION."
5180  INPUT "INPUT YOUR DECISION :",Ch
5190  IF Ch=1 THEN C9
5200  IF (Ch=2) AND (Prog2=1) THEN C1    ! OVERLAY THE DESOP PROGRAM
5210  IF (Ch<1) AND (Ch>2) THEN GOSUB Err
5220  GOTO P20
5230  !  ----------------------------------------------------
5240  Z99: !                        ----- END -----
5250  !  ----------------------------------------------------
5260  END
```

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APPENDIX E

DESOP Program Listing

In the development of the DESOP program, Refs. 2, 7, 8, 9, and 10 were used.

```
100 !   *****************************************************************  *  *  *  *  *  *  *  *  *  *
105 !                                                                      *  *  *  *  *  *  *  *  *  *
110 !              DESOP
115 !
120 !        DESKTOP SEQUENTIAL UNCONSTRAINED MINIMIZATION
125 !              TECHNIQUE OPTIMIZATION PROGRAM
130 !
135 !                    by W. B. COLE
140 !              NAVAL POSTGRADUATE SCHOOL, MONTEREY, CALIFORNIA
145 !                    1980
150 !
155 !   *****************************************************************  *  *  *  *  *  *  *  *  *  *
160 !
165 ! DATE OF LAST REVISION : 8/29/80
170 ! PROGRAM FEATURES :
175 ! 1. SEARCH METHODS:
180 !       A. STEEPEST DECENT
185 !       B. FLETCHER-REEVES
190 !       C. BOTH OF WHICH ARE NORMALIZED
195 ! 2. ALPHA BOUND - UTILIZES THE GOLDEN SECTION TECHNIQUE TO LOCATE THE
200 !       FUNCTION MINIMUM. THE PREDICTED MINIMUM IS TESTES AGAINST THE
205 !       ACTUAL VALUE OF OBJ AT THAT POINT.
210 ! 3. A FOUR POINT CUBIC IS USED TO PREDICT THE MINIMUM.
215 ! 4. IF THE CUBIC FIT FAILS THERE IS A QUADRATIC BACKUP.
220 ! 5. ABOBJ1 IS ADJUSTED ON EACH ITERATION.
225 ! 6. THE DESIGN VARIABLES ARE NORMALIZED
230 !
235 Opt1: ! CONTROL POINT FOR TRANSFER OF PROGRAM CONTROL FROM INPUT ROUTINE TO
240 !       ! OPTIMIZER ROUTINE.
```

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```
245   !  -----------------------------------------------------------------

250   !  ----                                                       -----
255   !  ----            BEGIN MAIN PROGRAM                         -----
260   Opt2:   ! BEGIN
265   DIM X(30),G(30),Tmp(30),Param(50),Df(30),Dfo(30),Vlb(30),Vub(30),Dfo(30),Scal(30)
270   DIM Xsav(30),Gg(30),C(10),Xscal(30),Scal(30)
275   !  -----------------------------------------------------------------
280   !      READ CONTROL PARAMETERS AND INITIAL DESIGN VARIABLES
285   !  -----------------------------------------------------------------
290   DISP "READING CONTROL PARAMETERS AND DESIGN VARIABLES."
295   ASSIGN #1 TO P$
300   ASSIGN #2 TO D$
305   READ #1,1
310   READ #1;Ndv,Ncon,Iprint,Delfun,Dabfun,Itmax,Icndir,Fdch,Fdchm,Abobj1,Alpha
x
315   READ #1,3
320   READ #1;Irmax,Rz,Rmult,Expg,Nscal
325   READ #2,1
330   FOR I=1 TO Ndv
335   READ #2;X(I)
340   NEXT I
345   READ #2,2
350   FOR I=1 TO Ndv
355   READ #2;Vlb(I),Vub(I)
360   NEXT I
365   Niter=0
370   Ncal=0
375   Ncc=0
380   C(2)=Iprint
385   IF Iprint<0 THEN PRINTER IS 0
390   IF Iprint>=0 THEN PRINTER IS 16
395   IF Ncon=0 THEN Irmax=1
```

! INITIALIZE PROGRAM PARAMETERS

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```
400  FOR I=1 TO Ndv                                    ! SCALE THE DESIGN VARIABLES
405  Scal(I)=X(I)
410  IF Scal(I)<1 THEN Scal(I)=1
415  IF Nscal=0 THEN Scal(I)=1
420  Xscal(I)=X(I)/Scal(I)
425  Dfo(I)=0
430  NEXT I
435  !-------------------------------------------------------------------
440  !------------------- INITIAL DESIGN -----------------------------
445  !-------------------------------------------------------------------
450  DISP "EVALUATING THE OBJECTIVE AND CONSTRAINT FUNCTIONS AT X(0)."
455  Icalc=1                                           ! FIRST AND LAST FLAG
460  C(1)=Icalc
465  CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)
470  Ncal=Ncal+1
475  IF Ncon>0 THEN GOSUB Penalize
480  Icalc=2
485  Nscal=0                                           ! INITIALIZE SCALING COUNTER
490  C(1)=Icalc
495  !
500  Objsav=Obj
505  PRINTER IS 0
510  IF Iprint=6 THEN PRINTER IS 16
515  IF Iprint=6 THEN PRINT PAGE
520  IF Iprint=6 THEN GOTO 540
525  PRINT LIN(2)
530  PRINT "----------------------------------------------------
     ----------------"
535  PRINT LIN(3)
540  PRINT "                            INITIAL DESIGN                 "
545  PRINT LIN(2),"DESIGN VARIABLES : "
550  FOR I=1 TO Ndv
555  PRINT "X("&VHL$(I)&")=";X(I),
560  NEXT I
565  IF Ncon<=0 THEN GOTO 590
```

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```
570  PRINT LIN(2),"CONSTRAINTS : "
575  FOR I=1 TO Ncon
580  PRINT "G(";&VAL$(I)&")=";G(I),
585  NEXT I
590  PRINT LIN(2),"OBJECTIVE FUNCTION :"
595  PRINT "OBJ=";Obj,"OBJA=";Obja
600  IF Iprint>=0 THEN PRINTER IS 16
605  DISP "PRESS 'CONT' TO CONTINUE"
610  DISP "OPTIMIZER RUNNING"
615  O1: ! CONTINUE
620  !-----------------------------------------
625  !------ OUTER LOOP FOR PENALTY FUNCTION -----
630  !-----------------------------------------
635  FOR Itr=1 TO Irmax
640  Objsvr=Obj
645  Kount=0
650  Dfold2=1
655  !-----------------------------------------
660  !----- INNER LOOP, NO INCREASE IN PENALTY FUNCTION -----
665  !-----------------------------------------
670  FOR Itm=1 TO Itmax
675  Niter=Niter+1
680  Kount=Kount+1
685  IF Kscal<>0 THEN GOTO 720
690  FOR I=1 TO Ndv                    ! SCALE THE DESIGN VARIABLES
695  Scal(I)=Xscal(I)*Scal(I)
700  IF Scal(I)<1 THEN Scal(I)=1
705  IF Nscal=0 THEN Scal(I)=1
710  Xscal(I)=X(I)/Scal(I)
715  NEXT I
720  Kscal=Kscal+1
725  IF Kscal=Ndv+2 THEN Kscal=0
730  IF Iprint<0 THEN PRINTER IS 0
735  IF ABS(Iprint)>1 THEN PRINT LIN(2)
740  IF ABS(Iprint)>1 THEN PRINT "*********************************************"
     *********************************************
```

```
745    IF ABS(Iprint)>1 THEN PRINT LIN(1),"ITERATION NUMBER : ";Niter
750    !--------------------------------------------------------------------------
755    !     ----- EVALUATE THE GRADIENT OF THE OBJECTIVE FUNCTION AND ANY -----
760    !     ----- ACTIVE CONSTRAINTS AT X(0)                              -----
765    !--------------------------------------------------------------------------
770    DISP "CALCULATING THE GRADIENTS"
775    GOSUB Grad
780    !
785    IF ABS(Iprint)>3 THEN PRINT."GRADIENTS :"
790    FOR I=1 TO Ndv
795    IF ABS(Iprint)>3 THEN PRINT " DF(";VAL$(I)&")=";Df(I),
800    NEXT I
805    DISP "FINDING THE SEARCH DIRECTION"
810    !
815  O5:   !--------------- FIND THE SEARCH DIRECTION -----
820    !
825    Df2=0
830    Dfold2=0                                    ! INITIALIZE Df
835    FOR I=1 TO Ndv
840    Dfold2=Dfold2+Dfo(I)^2
845    Df2=Df2+Df(I)^2
850    NEXT I
855    IF Kount>1 THEN O2                          ! USE FLETCHER REEVES
860    !--------------------------------------------------------------------------
865    !     ----- CALCULATION OF THE SEARCH DIRECTION BY STEEPEST DECENT -----
870    !--------------------------------------------------------------------------
       !
875    Fact=1E-3
880    FOR I=1 TO Ndv
885    S(I)=-Df(I)                                 ! SEARCH DIRECTION
890    IF ABS(S(I))>Fact THEN Fact=ABS(S(I))       ! NORMALIZE SEARCH DIRECTION
895    Dfo(I)=Df(I)
900    NEXT I
905    FOR I=1 TO Ndv
910    S(I)=S(I)/Fact
915    NEXT I
920    IF ABS(Iprint)>2 THEN PRINT LIN(1),"SEARCH METHOD : STEEPEST DESCENT"
925    GOTO O3                                     ! BRANCH AROUND FLETCHER REEVES
```

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```
930 02:  ! CONTINUE
935  ! ------------------------------------------------------------------
940  ! -----CALCULATION OF SEARCH DIRECTION BY FLETCHER REEVES-----
945  ! ------------------------------------------------------------------
950     Beta=Df2*Fact/Dfold2
955     Fact=1E-3
960     FOR I=1 TO Ndv
965     S(I)=-Df(I)+Beta*S(I)    ! SEARCH DIRECTION
970     IF ABS(S(I))>Fact THEN Fact=ABS(S(I))
975     Dfo(I)=Df(I)
980     NEXT I
985     FOR I=1 TO Ndv
990     S(I)=S(I)/Fact                    ! NORMALIZE THE SEARCH DIRECTION
995     NEXT I
1000    IF ABS(Iprint)>2 THEN PRINT LIN(1), "SEARCH METHOD : FLETCHER REEVES"
1005 03: ! CONTINUE
1010    IF Kount>=Icndir THEN Kount=0
1015    FOR I=1 TO Ndv
1020    IF ABS(Iprint)>2 THEN PRINT "    S("&VAL$(I)&")=";S(I),
1025    NEXT I
1030  ! ------------------------------------------------------------------
1035  ! -----CALCULATE THE SLOPE OF THE OBJECTIVE FUNCTION AT X(0) WITH-----
1040  ! -----RESPECT TO ALPHA -----
1045  ! ------------------------------------------------------------------
1050    Dfdalp=0                          ! OBJECTIVE FUNCTION SLOPE S(I)
1055    FOR I=1 TO Ndv
1060    Dfdalp=Dfdalp+Df(I)*S(I)
1065    NEXT I
1070    IF ABS(Dfdalp)<1E-20 THEN GOTO 099    ! IF SLOPE IS 0 THEN STOP
1075    IF ABS(Iprint)>2 THEN PRINT LIN(1), "DFDALP = ";Dfdalp
1080    IF Dfdalp>0 THEN Kount=0
1085    IF Dfdalp>0 THEN PRINT "THE OBJECTIVE FUNCTION HAS A POSITIVE SLOPE."
1090    IF Dfdalp>0 THEN PRINT "RESTART THE SEARCH USING STEEPEST DECENT."
1095    IF Dfdalp>0 THEN OS               !START OVER WITH STEEPEST DECENT
```

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```
1100 ! -----------------------------------------------------------------
1105 ! ----- ESTIMATE ALPHA IN THE 1-D SEARCH -----
1110 ! -----------------------------------------------------------------
     !
1115 DISP "CALCULATING AN INITIAL ALPHA"
1120 !
1125 GOSUB Alpges
1126 IF Alp3<1E-12 THEN Alp3=1E-12
1130 IF ABS(Iprint)>2 THEN PRINT "ALPHA GUESS =";Alp3
1135 IF Iprint=6 THEN DISP "PRESS 'CONT' TO CONTINUE."
1140 IF Iprint=6 THEN PAUSE
1145 04: ! CONTINUE
1150 ! -----------------------------------------------------------------
1155 ! ----- CALCULATE ALPHA IN THE 1-D SEARCH -----
1160 ! -----------------------------------------------------------------
1165 !
1170 DISP "FINDING ALPHA "
1175 !
1180 GOSUB Alpbnd
1185 !
1190 ! -----------------------------------------------------------------
1195 ! ----- ITERATION RESULTS -----
1200 ! -----------------------------------------------------------------
1205 PRINT LIN(1),"RESULTS :"
1210 FOR I=1 TO Ndv
1215 X(I)=Xscal(I)*Scal(I)
1220 PRINT "X("&VAL$(I)&")=";X(I),
1225 NEXT I
1230 IF Ncon=0 THEN GOTO 1255
1235 PRINT LIN(1)
1240 FOR I=1 TO Ncon
1245 PRINT "G("&VAL$(I)&")=";G(I),
1250 NEXT I
1255 PRINT LIN(1),"OBJ = ";Obj,"OBJA = ";Obja
1260 DISP "PRESS 'CONT' TO CONTINUE"
```

```
1265  !-------------------------------------------------------------------
1270  !                 ----- CHECK FOR CONVERGENCE -----
1275  !-------------------------------------------------------------------
1280  !
1285  GOSUB Convrg
1290  !
1295  IF ABS(Iprint)>2 THEN PRINT "DEL=";Del,"CONI=";Coni,LIN(1),"ABOBJ=";Abobj
1
1300  IF Iprint=6 THEN PAUSE
1305  IF Coni>=2 THEN DISP "CONVERGENCE MET, INCREASE THE PENALTY FUNCTION."
1310  IF Coni>=2 THEN GOTO 1335          !IF CONVERGENCE IS SATISFIED TWICE
1315  Objsav=Obj                         !PROCEED TO INCREMENT RZ
1320  !                        NEXT Item
1325  !-------------------------------------------------------------------
1330  !
1335  Rz=Rz*Rmult                        ! INCREASE THE PENALTY FUNCTION
1340  Rc=Rc+1                            ! COUNTER ON PENALTY INCREASES
1345  IF ABS(Iprint)>=2 THEN PRINT "RZ HAS BEEN INCREASED ";Rc;" TIMES TO ";Rz
1350  FOR I=1 TO Ndv
1355  X(I)=Xscal(I)*Scal(I)
1360  NEXT I
1365  CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)
1370  Ncal=Ncal+1
1375  IF Ncon>0 THEN GOSUB Penalize
1380  GOSUB Convrg
1385  IF Coni>=3 THEN GOTO 099
1390  Coni=0
1395  !                        NEXT Itr
1400  !
1405  !-------------------------------------------------------------------
1410  !
1415  !          ----- OPTIMIZATION RESULTS -----
1420  099:  !
1425  !-------------------------------------------------------------------
1430  IF Iprint=6 THEN GOTO 1455
1435  PRINTER IS 0
1440  PRINT LIN(2)
```

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```
1445  PRINT "---------------------------------------------------------------"
      "---------"
1450  PRINT LIN(2)
1455  IF Iprint=6 THEN PRINT PAGE
1460  PRINT "                    OPTIMIZATION   RESULTS   "
1465  PRINT LIN(3),"FINAL DESIGN VARIABLES : "
1470  FOR I=1 TO Ndv
1475  X(I)=Xscal(I)*Scal(I)
1480  PRINT "X("&VAL$(I)&") = ";X(I),
1485  NEXT I
1490  IF Ncon<=0 THEN O6
1495  PRINT LIN(2),"FINAL CONSTRAINTS :"
1500  FOR I=1 TO Ncon
1505  PRINT "G("&VAL$(I)&")=";G(I),
1510  NEXT I
1515  O6:  PRINT LIN(2),"FINAL OBJECTIVE FUNCTION :"
1520  PRINT "OBJ=";Obj,"OBJA=";Obja
1525  PRINT LIN(2),"NUMBER OF ITERATIONS :";Niter
1530  PRINT LIN(2),"NUMBER OF TIMES ANALIZE CALLED :",Ncal
1535  PRINT LIN(2),"RZ HAS BEEN INCREASED ";Rz;" TIMES TO ";Rz
1540  ! PRINT ANY RESULTS SPECIFIED BY ANALIZE
1545  Icalc=3
1550  C(1)=Icalc
1555  CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)
1560  DISP "END OF PROGRAM."
1565  LOAD "OFCON",C8
1570  END
```

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```
1575  ! *************************************************************
1580  Grad:  !          ----- SUBROUTINE GRAD -----
1585  ! *************************************************************
1590  !
1595  !          -----STORE THE CURRENT VALUES OF THE ANALIZE SUBROUTINE -----
1600  !          -----------------------------------------------------------
1605  !
1610  Objsav=Obj
1615  IF Ncon<=0 THEN GOTO G1
1620  FOR J=1 TO Ncon
1625  Tmp(J)=G(J)
1630  NEXT J
1635  G1: ! CONTINUE
1640  !
1645  !          ----- CALCULATE THE GRADIENTS -----
1650  !          --------------------------------------
1655  FOR J=1 TO Ndv
1660  Xsav=Xscal(J)
1665  Dx=ABS(Xsav)*Fdch
1670  IF Dx<Fdchm THEN Dx=Fdchm
1675  Xscal(J)=Xscal(J)+Dx
1680  !          ----- CALCULATE THE FUNCTION AT X(J) + DX(J) -----
1685  !          ----------------------------------------------------
1690  X(J)=Xscal(J)*Scal(J)
1695  CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)     ! CONVERT TO REAL X(*) TO ANALIZE
1700  Ncal=Ncal+1
1705  IF Ncon>0 THEN GOSUB Penalize
1710  !
1720  Df(J)=(Obj-Objsav)/Dx
```

```
1725 ! -------------------------------------------------------------
1730 !      ------ RETURN X(I) AND OBJ TO THEIR ORIGINAL VALUES -----
1735 ! -------------------------------------------------------------
1740    Xscal(J)=Xsav
1745    X(J)=Xscal(J)*Scal(J)
1750    NEXT J
1755    Obj=Objsav
1760    IF Ncon<=0 THEN GOTO G2
1765    FOR J=1 TO Ncon
1770    G(J)=Tmp(J)
1775    NEXT J
1780 G2: ! CONTINUE
1785    RETURN
1790 !
```

```
1795 ! ****************************************************************
1800 Alpges: !           ----- SUBROUTINE ALPGES -----
1805 ! ****************************************************************
1810 ! --------------------------------------------------------------
1815 ! --------- CALCULATE AN INITIAL ESTIMATE FOR ALPHA IN THE 1-D SEARCH
1820 !
1825 ! --------------------------------------------------------------
1830 Denom=ABS(Dfdalp)
1835 Anum=ABS(Obj)
1840 IF Denom<1E-5 THEN Denom=1E-5        ! PROTECT AGAINST DIVISION BY 0
1845 IF Anum<1 THEN Anum=1                ! PROTECT AGAINST A SMALL NUMERATOR
1850 Alp3=Abobj1*Anum/Denom               ! ALP3 = PRESENT UPPER BOUND
1855 FOR I=1 TO Ndv
1860 Axi=ABS(Xscal(I))
1865 IF Axi<1 THEN Axi=1
1870 Asi=ABS(S(I))
1875 IF Asi<1E-5 THEN Asi=1E-5
1880 Alp=Alphax*Axi/Asi
1885 IF Alp<Alp3 THEN Alp3=Alp
1890 NEXT I
```

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```
1895 ! -------------------------------------------
1900 ! ----- CHECK TO SEE IF ANY SIDE CONSTRAINTS ARE VIOLATED -----
1905 ! -------------------------------------------
1910 FOR I=1 TO Ndv
1915 Vlscal(I)=Vlb(I)/Scal(I)
1920 Vuscal(I)=Vub(I)/Scal(I)
1925 IF ABS((Xscal(I)-Vlscal(I))>1E50 THEN Ag1
1930 IF ABS((S(I))<1E-20 THEN Ag1
1935 Alp=(Xscal(I)-Vlscal(I))/S(I)
1940 IF ABS(Alp)<ABS(Alp3) THEN Alp3=Alp
1945 Ag1: !
1950 IF ABS((Xscal(I)-Vuscal(I))>1E50 THEN Ag2
1955 IF ABS(S(I)) THEN Ag2
1960 Alp=(Vuscal(I)-Xscal(I))/S(I)
1965 IF ABS(Alp)<ABS(Alp3) THEN Alp3=Alp
1970 Ag2: !
1975 Alp3=ABS(Alp3)
1980 NEXT I
1985 !
1990 RETURN
1995 !
```

```
2000 ! *********************************************************
2005 Alpbnd:  !          ----- SUBROUTINE ALPBND -----
2010 ! *********************************************************
2015 !----
2020 !----                ----- FIND ALPHA -----
2025 !----
2030 !----
2035 !----
2040 IF ABS(Iprint)>4 THEN PRINT "SUBROUTINE : ALPBND"
2045 IF ABS(Iprint)=5 THEN PRINT "DETERMINING THE UPPER AND LOWER BOUNDS ON AL
PHA."
2050 !----
2055 !----           ----- SAVE INPUT PARAMETERS -----
2060 !----
2065 Objsav=Obj
2070 FOR I=1 TO Ndv
2075 Xsav(I)=Xscal(I)
2080 NEXT I
2085 IF Ncon<=0 THEN GOTO A1
2090 FOR I=1 TO Ncon
2095 Tmp(I)=G(I)
2100 NEXT I
2105 A1:  ! CONTINUE
2110 !----
2115 !----              ----- INITIAL BOUNDS -----
2120 !----
2125 Alpz=0
2130 Fz=Obj
2135 A6:  ! TRANSFER
2140 FOR I=1 TO Ndv
2145 Xscal(I)=Xsav(I)+Alp3*S(I)
2150 X(I)=Xscal(I)*Scal(I)
2155 NEXT I
2160 !
2165 CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)
2170 Ncal=Ncal+1
2175 IF Ncon>0 THEN GOSUB Penalize
2180 F3=Obj
```

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```
2185  IF ABS(Iprint)>4 THEN PRINT "INITIAL BOUNDS."
2190  IF ABS(Iprint)>4 THEN PRINT "ALPHA2=";Alp2,"F2=";F2
2195  IF ABS(Iprint)>4 THEN PRINT "ALPHA3=";Alp3,"F3=";F3
2200  !
2205  ! IF F3 IS GREATER THEN F2 THE MIN. EXISTS BETWEEN ALP2 AND ALP3.
2210  IF F3>F2 THEN GOTO A3
2215  !
2220  A2: !      ----- INCREASE THE BOUNDS ON ALPHA -----
2225  !
2230  D1=Alp3-Alp2
2235  Alp1=Alp3
2240  F1=F3
2245  Alp3=Alp2+D1/.3819660113               ! INCREMENT X(I) BY ALP3
2250  FOR I=1 TO Ndv
2255  Xscal(I)=Xsav(I)+Alp3*S(I)
2260  X(I)=Xscal(I)*Scal(I)
2265  NEXT I
2270  !
2275  CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)
2280  Ncal=Ncal+1
2285  IF Ncon>0 THEN GOSUB Penalize
2290  F3=Obj
2295  IF ABS(Iprint)>4 THEN PRINT "INCREASE THE BOUNDS ON ALPHA"
2300  IF ABS(Iprint)>4 THEN PRINT "ALPHA2=";Alp2,"F2=";F2
2305  IF ABS(Iprint)>4 THEN PRINT "ALPHA1=";Alp1,"F1=";F1
2310  IF ABS(Iprint)>4 THEN PRINT "ALPHA3=";Alp3,"F3=";F3
2315  !
2320  ! IF OBJ IS GREATER THAN F1
2325  ! THE MINIMUM EXISTS BETWEEN ALP2 AND ALP3.
2330  ! PROCEED TO LOCALIZE THE MINIMUM.
2335  ! OTHERWISE INCREASE THE UPPER AND LOWER BOUNDS
2340  ! AND PROCEED TO SEARCH FOR THE MINIMUM.
2345  !
2350  IF F3>F1 THEN GOTO A4
2355  F2=F1
2360  Alp2=Alp1
2365  GOTO A2
2370  !
```

```
2375 A3: ! CALCULATE ALPHA1 AND F1
2380     D1=Alp3-Alpz
2385     Alp1=Alpz+D1*.3819660113
2390     FOR I=1 TO Ndv
2395     Xscal(I)=Xsav(I)+Alp1*S(I)
2400     X(I)=Xscal(I)*Scal(I)
2405     NEXT I
2410     CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)
2415     Ncal=Ncal+1
2420     IF Ncon>0 THEN GOSUB Penalize
2425     F1=Obj
2430     IF F1>Fz THEN Alp3=Alp1    ! RESTART BRACKETING THE MIN
2435     IF F1>Fz THEN GOTO A6
2440     !
2445 A4: ! CONTINUE
2450     !-------------------------------------------------------
2455     !-------- THE MINIMUM IS BRACKETED -----
2460     !-------------------------------------------------------
2465     IF ABS(Iprint)=5 THEN PRINT "THE MINIMUM IS BRACKETED - PROCEED TO LOCALIZE IT."
2470     D1=Alp3-Alpz
2475     Alp2=Alpz+.6180339887*D1
2480     ! CALCULATE F2
2485     FOR I=1 TO Ndv
2490     Xscal(I)=Xsav(I)+Alp2*S(I)
2495     X(I)=Xscal(I)*Scal(I)
2500     NEXT I
2505     CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)
2510     IF Ncon>0 THEN GOSUB Penalize
2515     Ncal=Ncal+1
2520     F2=Obj
2525 A5: ! TEST FOR LOCALIZATION.
2530     IF ABS(Iprint)>4 THEN PRINT "LOCALIZE THE MINIMUM"
2535     IF ABS(Iprint)>4 THEN PRINT "ALPHAZ=";Alpz,"FZ=";Fz
2540     IF ABS(Iprint)>4 THEN PRINT "ALPHA1=";Alp1,"F1=";F1
2545     IF ABS(Iprint)>4 THEN PRINT "ALPHA2=";Alp2,"F2=";F2
2550     IF ABS(Iprint)>4 THEN PRINT "ALPHA3=";Alp3,"F3=";F3
```

```
2555 ! -----------------------------------------------------------
2560 ! ----- TEST THE VERTICAL DIFFERENCE ON THE FOUR F's -----
2565 ! -----------------------------------------------------------
2570 IF (ABS((Fz-F1)/F1)>.1) OR (ABS((Fz-F2)/F2)>.1) THEN GOTO A11
2575 IF (ABS((F3-F1)/F1)>.1) OR (ABS((F3-F2)/F2)>.1) THEN GOTO A11
2580 !
2585 ! TEST TO SEE IF THE CUBIC INTERPOLATOR WILL GIVE A GOOD
2590 ! APPROXIMATION FOR THE MINIMUM ALPHA.
2595 !
2600 GOSUB Cuebic
2605 Objq=A0+A1*Alpha+A2*Alpha^2+A3*Alpha^3
2610 ! CALCULATE OBJ AT THE ALPHA GIVEN
2615 FOR I=1 TO Ndv
2620 Xscal(I)=Xsav(I)+Alpha*S(I)
2625 X(I)=Xscal(I)*Scal(I)
2630 NEXT I
2635 CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)
2640 IF Ncon>0 THEN GOSUB Penalize
2645 Ncal=Ncal+1
2650 A10: ! TEST THE TWO RESULTS FOR AGREEMENT
2655 IF ABS(Iprint)>2 THEN PRINT "OBJ=";Obj;"        OBJQ=";Objq
2660 IF ABS((Objq-Obj)/Obj)<1E-3 THEN GOTO A7
2665 IF Di<1E-3 THEN GOTO A7
2670 !
2675 A11: ! ----- PROCEDE WITH THE GOLDEN SEARCH FOR THE MINIMUM -----
2680 !
2685 IF Di<1E-12 THEN GOTO A7       ! EVEN THOUGH MIN NOT FOUND - EXIT
2690 IF F1>F2 THEN GOTO A12
2695 IF ABS(Iprint)=5 THEN PRINT "F1<F2"
2700 Alp3=Alp2
2705 F3=F2
2710 Alp2=Alp1
2715 F2=F1
2720 Di=Alp3-Alpz
2725 Alp1=Alpz+.3819660113*Di
```

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```
2730    ! CALCULATE F1
2735    FOR I=1 TO Ndv
2740    Xscal(I)=Xsav(I)+Alp1*S(I)
2745    X(I)=Xscal(I)*Scal(I)
2750    NEXT I
2755    CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)
2760    IF Ncon>0 THEN GOSUB Penalize
2765    Ncal=Ncal+1
2770    F1=Obj
2775    GOTO A5
2780    !
2785    A12: ! CONTINUE
2790    IF ABS(Iprint)=5 THEN PRINT "F1 >= F2"
2795    Alpz=Alp1
2800    Fz=F1
2805    Alp1=Alp2
2810    F1=F2
2815    D1=Alp3-Alpz
2820    Alp2=Alpz+.618033988*D1
2825    ! CALCULATE F2
2830    FOR I=1 TO Ndv
2835    Xscal(I)=Xsav(I)+Alp2*S(I)
2840    X(I)=Xscal(I)*Scal(I)
2845    NEXT I
2850    CALL Analiz(X(*),G(*),Gg(*),C(*),Obj)
2855    IF Ncon>0 THEN GOSUB Penalize
2860    Ncal=Ncal+1
2865    F2=Obj
2870    GOTO A5
2875    !
2880    A7: ! CONTINUE
2885    !
2890    RETURN
2895    !
2900    !
```

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```
2905  ! *********************************************************
2910  Quebic: !          ----- SUBROUTINE QUEBIC -----
2915  ! *********************************************************
2920  !
2925  !
2930  ! ROUTINE TO ESTIMATE THE ALPHA AT WHICH OBJ IS A MINIMUM BASED
2935  ! ON FOUR POINT CUBIC INTERPOLATION.
2940  !-------------------------------------------------------
2945  IF ABS(Iprint)>5 THEN GOTO 2975
2950  PRINT "CUBIC INTERPOLATOR INPUT"
2955  PRINT "ALPHAZ=";Alpz, "FZ=";Fz
2960  PRINT "ALPHA1=";Alp1, "F1=";F1
2965  PRINT "ALPHA2=";Alp2, "F2=";F2
2970  PRINT "ALPHA3=";Alp3, "F3=";F3
2975  O1=Alpz^3*(Alp2-Alp1)-Alp1^3*(Alp2-Alpz)+Alp2^3*(Alp1-Alpz)
2980  O2=Alpz^3*(Alp3-Alp1)-Alp1^3*(Alp3-Alpz)+Alp3^3*(Alp1-Alpz)
2985  O3=(Alp2-Alp1)*(Alp1-Alpz)*(Alp1-Alpz)*(Alp2-Alpz)
2990  O4=(Alp3-Alp1)*(Alp1-Alpz)*(Alp1-Alpz)*(Alp3-Alpz)
2995  Denq=O2*O3-O1*O4
3000  O5=F2*(Alp1-Alpz)-F1*(Alp2-Alpz)+Fz*(Alp2-Alp1)
3005  O6=F3*(Alp1-Alpz)-F1*(Alp3-Alpz)+Fz*(Alp3-Alp1)
3010  A3=(O3*O6-O4*O5)/Denq
3015  A2=(O5-O1*A3)/O3
3020  A1=(F1-Fz-A3*(Alp1^3-Alpz^3)/(Alp1-Alpz)-A2*(Alpz+Alp1)
3025  A0=Fz-A1*Alpz-A2*Alpz^2-A3*Alpz^3
3030  IF A3=0 THEN GOTO O10
3035  !
3040  ! THE GENERAL EQUATIONS OF THE FUNCTION ARE THEN
3045  ! Y = A0 + A1*X + A2*X^2 + A3*X^3
3050  ! dY/dX = A1 + 2*A2*X + 3*A3*X^2
3055  ! d2Y/dX2 = 2*A2 + 6*A3*X
3060  ! FIND THE MINIMUM USING FIRST AND SECOND DERIVATIVES.
3065  !-------------------------------------------------------
```

135

```
3070 ON ERROR GOTO 3080
3075 Xx1=(-A2+(A2^2-3*A1*A3)^.5)/(3*A3)
3080 OFF ERROR
3085 ON ERROR GOTO 3095
3090 Xx2=(-A2-(A2^2-3*A1*A3)^.5)/(3*A3)
3095 OFF ERROR
3100 Y2p=2*A2+6*A3*Xx1
3105 IF Y2p>0 THEN Alpha=Xx1
3110 IF Y2p<0 THEN Alpha=Xx2
3115 IF (Alpha>Alpz) AND (Alpha<Alp3) THEN GOTO Q1
3120 ! -------
3125 ! ----- THE PRIDICTED MINIMUM IS OUTSIDE THE BRACKETED MINIMUM -----
3130 ! -------
3135 IF F1>F2 THEN GOTO 02
3140 ! F1<F2 :  FIND THE MINIMUM USING A QUADRATIC FIT
3145 W1=(Alp1-Alpz)*(F2-Fz)-(Alp2-Alpz)*(F1-Fz)
3150 W2=(Alp1-Alpz)*(Alp2-Alpz)*(Alp2-Alp1)
3155 W3=W1/W2
3160 W4=(F1-Fz)/(Alp1-Alpz)-(Alpz+Alp1)*W3
3165 Alpha=-W4/(2*W3)
3170 GOTO 03
3175 02: ! F1 > F2 :   FIND THE MINIMUM USING A QUADRATIC FIT
3180 W1=(Alp2-Alp1)*(F3-F1)-(Alp3-Alp1)*(F2-F1)
3185 W2=(Alp2-Alp1)*(Alp3-Alp1)*(Alp3-Alp2)
3190 W3=W1/W2
3195 W4=(F2-F1)/(Alp2-Alp1)-(Alp1+Alp2)*W3
3200 Alpha=-W4/(2*W3)
3205 GOTO 03
```

```
3210 Q1:    IF ABS(Iprint)<5 THEN GOTO 3260
3215       PRINT "CUBIC OUTPUT"
3220       PRINT "Q1=";Q1, "Q2=";Q2
3225       PRINT "Q3=";Q3, "Q4=";Q4
3230       PRINT "Q5=";Q5, "Q6=";Q6
3235       PRINT "A0=";A0, "A1=";A1
3240       PRINT "A2=";A2, "A3=";A3
3245       PRINT "XX1=";XX1, "XX2=";Xx2
3250       PRINT "Y2P=";Y2p
3255 Q3:    IF ABS(Iprint)>2 THEN PRINT "ALPHA=";Alpha
3260       RETURN
3265 Q10:   ! IF A3=0 THEN THE FUNCTION IS A QUADRATIC
3270       Alpha=-A1/(2*A2)
3275       IF ABS(Iprint)<5 THEN GOTO 3295
3280       PRINT "THE FUNCTION IS A QUADRATIC"
3285       PRINT "A1=";A1, "A2=";A2
3290       PRINT "ALPHA=";Alpha
3295       RETURN
3300       !
```

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```
3305 ! *****************************************************************
3310 Convrg: !        ----- SUBROUTINE CONVRG -----
3315 ! *****************************************************************
3320 !-----------------------------------------------------------------
3325 !-----------------------------------------------------------------
3330 !              CHECK ON CONVERGENCE CRITERIA
3335 !-----------------------------------------------------------------
3340 !-----------------------------------------------------------------
3345 Del=ABS((Obj-Objsav)/Obj)
3350 Abobj1=(Abobj1+Del)/2
3355 IF Del<Delfun THEN Coni=Coni+1       ! INCREASE CONVERGENCE COUNTER BY 1
3360 IF Del<Delfun THEN Kount=0           ! NEXT ITERATION - STEEPEST DECENT
3365 IF Del<Delfun THEN RETURN
3370 IF ABS(Obj-Objsav)<Dabfun THEN Coni=Coni+1
3375 IF ABS(Obj-Objsav)<Dabfun THEN Kount=0
3380 Objsav=Obj
3385 RETURN
3390 !-
3395 !-
```

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```
3400 ! *****************************************************
3405 Penalize:!       ----- SUBROUTINE PENALIZE -----
3410 ! *****************************************************
*
3415     Obj=Obj
3420 ! -----------------------------------------------------
3425 !       ----- ADD PENALTIES FOR VIOLATED CONSTRAINTS. -----
3430 ! -----------------------------------------------------
3435     FOR I=1 TO Ncon
3440     Gi=G(I)
3445     IF Gi>0 THEN Obj=Obj+Rz*Gi^Expg
3450     NEXT I
3455 ! -----------------------------------------------------
3460 Penal1: !   ----- ADD PENALTIES FOR VIOLATED SIDE CONSTRAINTS. -----
3465 ! -----------------------------------------------------
3470     FOR I=1 TO Ndv
3475     X(I)=X(I)*Scal(I)
3480     IF X(I)<Vlb(I) THEN Obj=Obj+Rz*((Vlb(I)-X(I))/X(I))^Expg
3485     IF X(I)>Vub(I) THEN Obj=Obj+Rz*((X(I)-Vub(I))/Vub(I))^Expg
3490     NEXT I
3495     RETURN
3500 !
3505 !
3510 !
3515 !
3520 !
3525 Analiz1:   ! ATTACHMENT POINT FOR ANALIZE ROUTINE.
3530 !
3535     END
```

```
100 SUB Analiz(X(*),G(*),Gg(*),C(*),Obj)
110 !
120 ! ----- BANANA FUNCTION -----
130 !
140 ! A TEST PROGRAM FOR OPTIMIZER DEVELOPEMENT
150 ! THERE ARE NO CONSTRAINTS ON THE BANANA FUNCTION.
160 ! THERE ARE NO SIDE CONSTRAINTS ON THE BANANA FUNCTION.
170 !     NDV = 2
180 !     NCON = 0
190 ! RECOMMENDED STARTING VALUES ARE:
200 !     X(1) = -1.2
210 !     X(2) = 1.0
220 !     TRUE MINIMUM = 4.00
230 !
240 !------------------------------------------------
250 !
260 ! DESIGN VARIABLES :
270 X1=X(1)
280 X2=X(2)
290 ! OBJECTIVE FUNCTION :
300 Obj=10*(X2-X1^2)^2+(1-X1)^2+4
310 SUBEND
```

```
100   SUB Analiz(X(*),G(*),Gg(*),C(*),Obj))
110   !
120   !---------              ROSEN-SUZUKI FUNCTION
130   !---------       A CONSTRAINED OPTIMIZATION PROBLEM         ---------
140   !
150   ! A TEST PROGRAM FOR OPTIMIZER DEVELOPEMENT
160   ! THERE ARE NO SIDE CONSTRAINTS ON THE ROSEN-SUZUKI FUNCTION.
170   !    NDV = 4
180   !    NCON = 3
190   !    RECOMMENDED STARTING VALUES:
200   !       ALL X(I) = 1
210   !    TRUE MINIMUM = 6.00
220   !
230   !
240   !
250   ! DESIGN VARIABLES :
260   X1=X(1)
270   X2=X(2)
280   X3=X(3)
290   X4=X(4)
300   ! OBJECTIVE FUNCTION :
310   Obj=X1^2-5*X1+X2^2-5*X2+2*X3^2-21*X3+X4^2+7*X4+50
320   ! CONSTRAINTS
330   G(1)=X1^2+X1+X2^2-X2+X3^2+X3+X4^2-X4-8
340   G(2)=X1^2-X1+2*X2^2+X3^2+2*X4^2-X4-10
350   G(3)=2*X1^2+2*X1+X2^2-X2+X3^2-X4-5
360   !
370   SUBEND
```

```
100  SUB Analiz(X(*),G(*),Gg(*),C(*),Obj)
110  GOTO 490
120  !
130  !
140  !
150  !              "TSVAR"
160  !
170  ! Himmelblau, D. M. , Applied Nonlinear Programming, McGraw Hill Book
180  !    Co., San Francisco, 1972, pp.410-412
190  !
200  !      A CONSTRAINED OPTIMIZATION PROBLEM
210  !
220  ! CODED BY : Walter B. Cole, June 9, 1980
230  !
240  !   NDV = 5
250  !   NCON = 6
260  ! THERE ARE 10 SIDE CONSTRAINTS
270  !.RECOMMENDED STARTING VALUES ARE :
280  !   X(1) = 2.52
290  !   X(2) = 2
300  !   X(3) = 37.5
310  !   X(4) = 9.25
320  !   X(5) = 6.8
330  ! SIDE CONSTRAINTS TO BE ENTERED ON INPUT
340  !   1.    0 <= X1 <= 5
350  !   2.    1.2 <= X2 <= 2.4
360  !   3.    20 <= X3 <= 60
370  !   4.    9 <= X4 <= 9.3
380  !   5.    6.5 <= X5 <= 7
390  !
400  ! FINAL RESULTS :
410  !   OBJ  = -5280254
420  !   X(1) = 4.538
430  !   X(2) = 2.400
440  !   X(3) = 60.000
450  !   X(4) = 9.300
     !   X(5) = 7.000
```

```
460  ! -------------------
470  ! -------------------
480  ! DESIGN VARIABLES :
490  X1=X(1)
500  X2=X(2)
510  X3=X(3)
520  X4=X(4)
530  X5=X(5)
540  ! -------------------
550  ! CONSTANTS :
560  K1=-145421.402
570  K2=2931.1506
580  K3=-40.427932
590  K4=5106.192
600  K5=15711.35
610  K6=-161622.577
620  K7=4176.15328
630  K8=2.8260078
640  K9=9200.476
650  K10=13160.295
660  K11=-21686.9194
670  K12=123.56928
680  K13=-21.11888894
690  K14=706.834
700  K15=2848.573
710  K16=28298.388
720  K17=60.81096
730  K18=31.242116
740  K19=329.574
750  K20=-2882.082
760  K21=74095.3845
770  K22=-306.262544
780  K23=16.243649
790  K24=-3094.252
800  K25=-5566.2628
810  K26=-26237
820  K27=99
```

```
830 K28=-.42
840 K29=1300
850 K30=2100
860 K31=925548.252
870 K32=-61968.8432
880 K33=23.3088196
890 K34=-27097.648
900 K35=-50843.766
910 '
920 X6=(K1+K2*X2+K3*X3+K4*X4+K5*X5)*X1
930 Y1=K6+K1*X2+K8*X3+K9*X4+K10*X5
940 Y2=K11+K12*X2+K13*X3+K14*X4+K15*X5
950 Y3=K16+K17*X2+K18*X3+K19*X4+K20*X5
960 Y4=K21+K22*X2+K23*X3+K24*X4+K25*X5
970 X7=(Y1+Y2+Y3)*X1
980 X8=(K26+K27*X2+K28*X3+K29*X4+K30*X5)*X1+X6+X7
981 Icalc=C(1)
990 IF Icalc>1 THEN GOTO 1080
1000 PRINTER IS 0
1010 PRINT "          TSVAR INTERNAL PARAMETERS"
1020 PRINT LIN(2),"X6=";X6,"Y1=";Y1
1030 PRINT "Y2=";Y2,"Y3=";Y3
1040 PRINT "Y4=";Y4,"X7=";X7
1050 PRINT "X8=";X8
1060 PRINTER IS 16
1070 '
1080 ' OBJECTIVE FUNCTION :
1090 Max=(50*Y1+9.583*Y2+26*Y3+15*Y4-852960-38100*(X2+.01*X3)+K31+K32*X2+K33*X3
+K34*X4+K35*X5)*X1-24345+15*X6
1100 Obj=-Max
```

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```
1110 :
1120 : CONSTRAINTS :
1130 G(1)=-X6
1140 G(2)=X6-294000
1150 G(3)=-X7
1160 G(4)=X7-294000
1170 G(5)=-X8
1180 G(6)=X8-277200
1190 :
1200 :
1210 SUBEND
```

```
100   SUB Analiz(X(*),G(*),Gg(*),C(*),Obj)
110   !
120   !          "T7VAR"
130   !
140   !      A CONSTRAINED OPTIMIZATION PROBLEM
150   !
160   ! Kuester, J. L., and Mize, J. H.,  Optimization Techniques,
170   !      McGraw Hill, San Francisco 1973, pp.73-74.
180   !
190   ! A TEST PROGRAM FOR OPTIMIZER DEVELOPEMENT.
200   !      NDV = 7
210   !      NCON = 1
220   !      SIDE CONSTRAINTS: ALL X(I) > 0
230   !      TRUE MINIMUM = -200
240   !
250   !
260   !
270   ! NOTE : SIDE CONSTRAINTS ENTERED ON INPUT, ALL X(I) > 0
280   !
290   ! DESIGN VARIABLES :
300   ! X1=X(1)
310   ! X2=X(2)
320   ! X3=X(3)
330   ! X4=X(4)
340   ! X5=X(5)
350   ! X6=X(6)
360   ! X7=X(7)
370   ! OBJECTIVE FUNCTION :
380   Obj=-60*X1-60*X2-40*X3-10*X4-20*X5-10*X6-3*X7
390   ! CONSTRAINTS :
400   G(1)=-10+3*X1+5*X2+4*X3+1*X4+4*X5+3*X6+1*X7
410   ! SIDE CONSTRAINTS : TO BE ENTERED ON INPUT
420   !      ALL X(I) >= 0
430   !
440   SUBEND
```

APPENDIX G

NISCO Subprogram Listing

Below is a cross reference list of major equations used in the NISCO program to the references used to develop the equations.

Reference Number	NISCO Subprogram Line Number
3.	820 - 850
4.	1085 - 1090
5.	915, 985 - 1045
6.	855, 925, 930, 965 - 980, 1100, 1180 - 1210, 1255 - 1345, 1460, 1465,
11.	905, 1115, 1125, 1145
12.	1445 - 1455, 1470 - 1480
13.	1600 - 1605

```
100  SUB Analiz(X(*),G(*),Gg(*),C(*),Obj)
105  !
110  !  *****************************************************************
115  !  *                                                             *
120  !  *                         HISCO                               *
125  !  *                                                             *
130  !  *       AN OPTIMIZATION ANALYSIS PROGRAM FOR A                *
135  !  *       NONIMAGING COMPOUND PARABOLIC TROUGH                  *
140  !  *       CONCENTRATING SOLAR COLLECTOR.                        *
145  !  *                                                             *
150  !  *             by WALTER B. COLE                               *
155  !  *       NAVAL POST GRADUATE SCHOOL, MONTEREY, CA.             *
160  !  *             1980                                            *
165  !  *                                                             *
170  !  *                                                             *
175  !  *****************************************************************
180  DIM De(13),Mhid(13),Ib(13,10),Alts(13,10),Azm(13,10),Iamb(13),Drf(13)
185  !
190  Icalc=C(1)                        ! OPTIMIZER FLAG FOR 1st AND LAST RUN
195  Pi=3.141592654
200  Ncal=Ncal+1                       ! ITERATION COUNTER
205  Thetai=X(1)*PI/180                ! MAXIMUM ACCEPTANCE ANGLE (Radians)
210  Thetat=X(2)*PI/180                ! TRUNCATED THETA (Radians)
215  R=X(3)/12                         ! RECEIVER RADIUS (Feet)
220  L=X(4)                            ! RECEIVER LENGTH (Feet)
225  Mfr=X(5)                          ! MASS FLOW RATE (lbm/Hour)
230  !
235  !  ------ CONSTANTS ------
240  N1:  !
245  !
250  Lat=40*PI/180                     ! 40 DEGREES NORTH LATITUDE
255  Awall=0                           ! WALL AZIMUTH ANGLE w/r TO SOUTH
260  Alpr=.93                          ! RECEIVER ABSORPTIVITY (OXIDIZED Cu)
265  Eptr=.40                          ! RECEIVER EMISSIVITY (THERMAL RAD.)
270  Rhor=.07                          ! RECEIVER REFLECTIVITY
275  Rhom=.89                          ! REFLECTOR REFLECTIVITY (VACUUM
280                                    !   DEPOSITED AI ON RESIN)
```

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```
285  Alpab=.03              ! COVER AVERAGE ABSOPTANCE
290  Taub=.8                ! COVER AVERAGE TRANSMITTANCE
295  Rhog=.17               ! COVER AVERAGE REFLECTIVITY
300  Sbc=1.714E-9           ! STEPHAN BOLTZMAN CONSTANT
305                         ! ( BTU/(Hr Ft^2 R^4) )
310  Gc=32.2                ! GRAVITY CONSTANT
315  Epta=.94               ! COVER EMISSIVITY (THERMAL RAD.)
320  Vp=3                   ! VAPOR PRESSURE (mm Hg)
325  A3=.68                 ! LATITUDE FUNCTION
330  Cc=0                   ! CLOUD COVER (TENTHS)
335  Rhab=.07               ! COVER AVERAGE REFLECTIVITY
340  Tci=100                ! COOLANT INLET TEMP TO RECIEVER (F)
345  Sg=.87                 ! COOLANT SPECIFIC GRAVITY
350  Zzz=1                  ! ITERATION COUNTER
355  Iprint=7               ! PRINTER CONTROL
360  Dt=.0001               ! CONVERGENCE CRITERIA (Tdchm/100)
365  Nyr=20                 ! NUMBER OF YEARS
370  Cac=22.5               ! COLLECTOR COST ( $/ft^2 )
375  Cf=8.14E-6             ! FUEL COST ( $/Btu ) FOR GAS
380  Ia=.1                  ! ANNUAL INFLATION RATE
385  If=.11                 ! ANNUAL FUEL INFLATION RATE
390  Dtcm=10                ! MINIMUM CHANGE IN COOLANT TEMP
395  -
400  - !----------------------------------------- DATA ------
405  M2:  -   !-----------------------------------------------
410       -   !-----------------------------------------------
415       ! Dc(M) - SOLAR DECLINATION (MONTH)
420       DATA -0.34907,-.188496,0,.20246,0.349066,0.409279,.35554,0.214675,0,-.1832
6,-.345575,-.409279
425       ! Nhid(M) - NUMBER OF SOLAR INSOLATION HOUR PERIODS / DAY (MONTH)
430       DATA 5,6,6,7,8,8,7,6,6,5,5
435       ! Ib(M,H) - TOTAL INSOLATION ON NORMAL SURFACE (MONTH,HOUR) (BTU/Ft^2)
```

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```
436  ! DATA FOR 40 deg NORTH LATTITUDE FROM ASHRAE HANDBOOK OF FUNDAMENTALS
440  DATA 294,289,274,239,142                          ! JAN. 21
445  DATA 308,305,295,274,224,69                       ! FEB. 21
450  DATA 307,305,297,282,250,171                      ! MAR. 21
455  DATA 293,292,286,274,252,206,89                   ! APR. 21
460  DATA 284,283,277,267,250,216,144,1                ! MAY. 21
465  DATA 279,277,272,263,246,216,155,22               ! JUN. 21
470  DATA 276,275,269,259,241,208,138,2                ! JUL. 21
475  DATA 280,278,272,260,237,191,81                   ! AUG. 21
480  DATA 290,287,280,263,230,143                      ! SEP. 21
485  DATA 294,291,280,257,204,48                       ! OCT. 21
490  DATA 288,283,268,232,136                          ! NOV. 21
495  DATA 285,280,261,217,89                           ! DEC. 21
500  ! Alts(M,H) - SOLAR ALTITUDE (MONTH,HOUR)
505  DATA 30,28.4,23.8,16.8,8.1                        ! JAN. 21
510  DATA 40,38.1,32.8,25.5,15.4,4.8                   ! FEB. 21
515  DATA 50,47.7,41.6,32.8,22.5,11.4                  ! MAR. 21
520  DATA 61.6,58.7,51.4,41.3,30.3,18.9,7.4            ! APR. 21
525  DATA 70,66.2,57.5,46.8,35.4,24.0,12.7,1.9         ! MAY. 21
530  DATA 73.5,69.2,59.0,47.9,37.4,26.0,14.8,4.2       ! JUN. 21
535  DATA 70.6,66.7,57.9,47.2,35.8,24.3,13.1,2.3       ! JUL. 21
540  DATA 62.3,59.3,51.2,41.8,30.7,19.3,7.9            ! AUG. 21
545  DATA 50.0,47.7,41.6,32.8,22.5,11.4                ! SEP. 21
550  DATA 39.5,37.6,32.4,24.5,15.0,4.5                 ! OCT. 21
555  DATA 30.2,28.6,24.0,17.0,8.2                      ! NOV. 21
560  DATA 26.6,25.0,20.7,14.0,5.5                      ! DEC. 21
565  ! Azm(M,H) - SOLAR AZIMUTH ANGLE (MONTH,HOUR)
570  DATA 0,16.9,44,55.3                               ! JAN. 21
575  DATA 0,18.9,35.9,50.2,62.2,72.7                   ! FEB. 21
580  DATA 0,22.6,41.9,57.3,69.6,80.2                   ! MAR. 21
585  DATA 0,29.2,51.4,67.2,79.3,89.5,98.9              ! APR. 21
590  DATA 0,37.1,60.9,76.0,87.2,96.6,105.6,114.7       ! MAY. 21
595  DATA 0,41.9,65.8,80.2,90.7,99.7,108.4,117.3       ! JUN. 21
600  DATA 0,37.9,61.7,76.7,87.8,97.2,106.1,115.2       ! JUL. 21
605  DATA 0,29.7,52.1,67.9,79.9,90.9,99.5              ! AUG. 21
610  DATA 0,22.6,41.9,57.3,69.6,80.2                   ! SEP. 21
615  DATA 0,18.7,35.6,49.6,61.9,72.3                   ! OCT. 21
620  DATA 0,16.1,31.0,44.1,55.4                        ! NOV. 21
625  DATA 0,15.2,29.4,41.9,53                          ! DEC. 21
```

```
630  ! Tamb(M) - AVERAGE DAILY TEMPERATURE (MONTH)
635  DATA 40,40,45,55,60,70,80,80,70,60,45,40
640  ! Drf(M) - DIFFUSE SOLAR RADIATION FACTOR (MONTH)
645  DATA 0.058,0.06,0.071,.097,.121,.134,.136,.122,.092,.073,.063,.057
650  ! READ INPUT DATA
655  FOR M=1 TO 12
660  READ Ds(M)
665  NEXT M
670  FOR M=1 TO 12
675  READ Nhid(M)
680  NEXT M
685  FOR M=1 TO 12
690  FOR H=1 TO Nhid(M)
695  READ Ib(M,H)
700  NEXT H
705  NEXT M
710  FOR M=1 TO 12
715  FOR H=1 TO Nhid(M)
720  READ Altsd
725  Alts(M,H)=Altsd*PI/180                         ! CHANGE TO RADIANS
730  NEXT H
735  NEXT M
740  FOR M=1 TO 12
745  FOR H=1 TO Nhid(M)
750  READ Azind
755  Azm(M,H)=Azind*PI/180
760  NEXT H
765  NEXT M
770  FOR M=1 TO 12
775  READ Tamb(M)
780  NEXT M
785  FOR M=1 TO 12
790  READ Drf(M)
795  NEXT M
800  !
```

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```
805 R3:   ! -------- COLLECTOR GEOMETRY --------
810 R3:   ! ------
815 !
820      T=R*(Thetat+Thetai+PI/2-COS(Thetat-Thetai)/(1+SIN(Thetat-Thetai))
825      Thetax=3*PI/2-Thetai                    ! THETA MAX.
830      Thetan=PI/2+Thetai                      ! THETA MIN.
835      At=2*(r*SIN(Thetat)-T+SIN(Thetat+PI/2)) ! APERATURE OPENING AREA
840      Ar=2*PI*r                               ! RECEIVER AREA
845      Cr=At/Ar                                ! CONCENTRATION RATIO
850      Cd=-R*COS(Thetat)+T+COS(Thetat+PI/2)    ! COLLECTOR DEPTH (ft)
855      Nbar=LOG(Cr*.5)                         ! AVERAGE NUMBER OF REFLECTIONS
865      Tr=150                  ! ASSUME AN INITIAL RECEIVER TEMP
870      Ta=100                  ! ASSUME AN INITIAL COVER TEMP
885 N4:  ! -------- MONTHLY CALCULATIONS --------
900      FOR M=1 TO 12
905      Betat=Thetai-Alt=(M,1)+PI/2             ! COLLECTOR TILT ANGLE
910      Betag=PI/2-Beta-Thetai                  ! MINIMUM ACCEPTED SOLAR ALTITUDE
915      Fsg=(1-COS(Beta))/2                     ! GROUND ANGLE FACTOR
920      ! SKY HEAT LOSS CONSTANTS.
925      Hsky=Epta*Sbc*(Tamb(M)+460)^4+(.39-.0096*(...)-4-Ept*Sbc*(Tamb(M)
    +460)^4
930      Bsky=4*Epta*Sbc*(Tamb(M)+460)^3
935 N5:  ! ------- HOURLY CALCULATIONS -------
950      FOR H=1 TO Nhid(M)
955      Hs=(H-1)*15*PI/180                      ! SOLAR HOUR ANGLE
960      ! Csi - COSINE OF THE ANGLE THE SUN MAKES WITH THE COVER NORMAL
965      Csi1=SIN(Dec(M))*SIN(Lat)*COS(Beta)-COS(Lat)*SIN(Beta)*COS(Awall))
970      Csi2=COS(Dec(M))*COS(He)*(COS(Lat)*COS(Beta)+SIN(Lat)*SIN(Beta)*COS(Awall))
975      Csi3=COS(Dec(M))*SIN(Beta)*SIN(Awall)*SIN(He)
980      Csi=Csi1+Csi2+Csi3
985      ! Hpct - PERCENTAGE OF A PARTIAL HOUR OF RADIATION
```

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990   Hpct=(Alts(M,H-1)-Beta9)/(Alts(M,H-1)-Alts(M,H))
995   ! Ibc - DIRECT BEAM RADIATION INCIDENT ON THE COVER
1000  Ibc=Ibc(M,H)*Csi
1005  IF Alts(M,H)<Beta9 THEN Ibc=Ibc*Hpct
1010  ! Idc - DIFFUSE BEAM RADIATION INCIDENT ON THE COVER
1015  Idc=Drf(M)*Ibc*(1-Fsg)
1020  ! Irc - REFLECTED BEAM RADIATION INCIDENT ON THE COVER
1025  Irc=Ibc*(Drf(M)+SIN(Alts(M,H)))*Rhog*Fsg
1030  ! Tauai - COVER TRANSMISIVITY AS A FUNCTION OF INCIDENT ANGLE
1035  Tauai=-.00885+2.71235*Csi-.62062*Csi^2-7.07329*Csi^3+9.75995*Csi^4-3.89922
*Csi^5
1040  ! Alpai - COVER ABSORPTANCE AS A FUNCTION OF INCIDENT ANGLE
1045  Alpai=.01154+.77674*Csi-3.94654*Csi^2+8.57881*Csi^3-9.38135*Csi^4+3.01168*
Csi^5
1050  Zzz=1
1055  ! ----                          ! ITERATION COUNTER
1060  H6:!
1063  ! ----- PERFORM A HEAT BALANCE ON THE COLLECTOR ------
1065  !
1070  Zzz=Zzz+1
1075  Trr=Trr+460
1080  Tac=Ta+460
1085  Cp=4.94E-4*Tr+.4035                    ! SPECIFIC HEAT FOR THERMINOL 55
1090  Viac=(-.053*Tr+32.3)*6.7195E-4         ! VISCOSITY (lbm/(ft sec))
1095  ! CALCULATE THE HEAT TRANSFER COEFFICIENTS.
1100  ! Hrar - RADIATION HEAT TRANSFER COEFFICIENT : COVER TO RECEIVER
1105  Hrar=Sbc*(Tcr+Tar)*(Tcr^2+Tar^2)/(1/Eptc+1/Epta-1)
1110  ! Hcra - CONVECTION HEAT TRANSFER COEFFICIENT : RECEIVER TO COVER
1115  Hcra=.21*(ABS(Tcr-Ta)/2*Ar)^.25
1120  ! Hcar - CONVECTION HEAT TRANSFER COEFFICIENT : COVER TO RECEIVER
1125  Hcar=.29*(ABS(Ta-Tr)/2*SIN(Beta9)/Ar)^.25
1130  ! Hcb - AVERAGE HEAT TRANSFER COEFFICIENT BETWEEN COVER AND RECEIVER
1135  Hcb=Hcra*Hcar/(Cr+(Hcar+Hcra/Cr))
1140  ! Hce - CONVECTION HEAT TRANSFER COEFFICIENT COVER TO ENVIRONMENT
1145  Hce=.29*(ABS(Ta-Tamb(M))*SIN(Beta9)/Ar)^.25+Cr
```

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```
1150 ! ------------------------------------------
1155 N7:! ----- PERFORM A HEAT BALANCE ON THE COVER AND SOLVE FOR TA -----
1160 ! ------------------------------------------
1165 !
1170 ! Qba - DIRECT SOLAR RADIATION ABSORBED BY THE COVER BOTH DIRECTLY AND
1175 !        INDIRECTLY AFTER REFLECTION FROM THE RECEIVER
1180 Qba=Ibc*(Alpai+Tauai*Rhom^(2*Nbar)*Rhor*Alpab)*Cr
1185 ! Qda - DIFFUSE SOLAR RADIATION ABSORBED BY THE COVER
1190 Qda=Idc*Alpab*Cr
1195 ! Qra - REFLECTED SOLAR RADIATION ABSORBED BY THE COVER
1200 Qra=Irc*Alpab*Cr
1205 ! Tap - NEW COVER TEMPERATURE
1210 Tap=(Qba+Qda+Qra-Asky-Bsky*460+Tr*(Hrar+Hcb)+Hce*Tamb(M))/(Hrar+Hcb+Bsky+H
ce)
1215 IF ABS(Tap>500) THEN Tap=70
1220 ! ------------------------------------------
1225 N8:! ----- PERFORM A HEAT BALANCE ON THE RECEIVER -----
1230 !       ----- AND SOLVE FOR THE USEFUL HEAT OUT -----
1235 ! ------------------------------------------
1240 !
1245 ! Qbr - DIRECT SOLAR RADIATION ABSORBED BOTH DIRECTLY AND INDIRECTLY
1250 !        BY THE RECEIVER AFTER REFLECTION FROM THE REFLECTOR
1255 Qbr=Ibc*Tauai*Rhom^Nbar*Alpr*(1+Rhom^(2*Nbar)*Rhor*Rhab)*Cr
1260 ! Qdr - DIFFUSE SOLAR RADIATION ABSORBED BY THE RECEIVER
1265 Qdr=Idc*Taub*Rhom^Nbar*Alpr
1270 ! Qrr - REFLECTED SOLAR RADIATION ABSORBED BY THE RECEIVER
1275 Qrr=Irc*Taub*Rhom^Nbar*Alpr
1280 ! Qcra - CONVECTIVE EXCHANGE BETWEEN THE RECEIVER AND THE COVER
1285 Qcra=Hcb*(Tr-Ta)
1290 ! Qir - RADIATIVE EXCHANGE BETWEEN THE RECEIVER AND THE COVER
1295 Qir=Hrar*(Tr-Ta)
1300 ! Qu - USEFUL HEAT EXTRACTION
1305 Qu=(Qbr+Qdr+Qrr-Qcra-Qir)*L*Ar
1310 !
```

```
1315   !  ------------------------------------------------------------------
1320   N9:!   -----  PERFORM A HEAT BALANCE ON THE WORKING FLUID  -----
1325   !       -----  AND SOLVE FOR THE NEW RECEIVER TEMP  -----
1330   !  ------------------------------------------------------------------
1335   !
1340   ! Tc2 - COOLANT EXIT TEMPERATURE
1345   Tc2=Qw/(Cp*Mfr)+Tc1
1350   IF (M=6) AND (H=1) THEN Tc21=Tc2
1355   ! Trp - NEW RECIEVER TEMPERATURE
1360   Trp=(Tc1+Tc2)/2
1365   IF ABS(Trp)>10000 THEN Trp=10000
1370   !  ------------------------------------------------------------------
1375   N10:!   -----  CHECK FOR CONVERGENCE OF Ta WITH Tap AND Tr WITH Trp  -----
1380   !  ------------------------------------------------------------------
1385   !
1390   IF (ABS((Ta-Tap)/Tap)<Dt) AND (ABS((Tr-Trp)/Trp)<Dt) THEN GOTO N11
1395   Ta=Tap
1400   Tr=Trp
1405   GOTO N6
1410   !
1415   N11:!  ! CONVERGENCE MET
1420   !
1425   !  ------------------------------------------------------------------
1430   N12:!     -----  CALCULATE PUMPING POWER REQUIRED  -----
1435   !  ------------------------------------------------------------------
1440   !
1445   Den=Sg*62.4                              ! COOLANT DENSITY (lbm/ft^3)
1450   Mv=Mfr/(PI*R^2)                          ! COOLANT MASS VELOCITY (lbm/hr/ft^2)
1455   Re=Mv*2*R/(Visc*3600)                    ! REYNOLDS NUMBER
1460   IF Re<2100 THEN Ff=16/Re                 ! FRICTION FACTOR
1465   IF Re>=2100 THEN Ff=.079*Re^(-.25)
1470   Vc=Mfr/(Den*PI*R^2*3600)                 ! COOLANT VELOCITY (ft/sec)
1475   Dpc=2*Ff*Den*Vc^2/(R*Gc)
1480   Ppc=Sg*Mfr*Dpc*1.84939E-2*L/Den          ! COLLECTOR PUMPING POWER (Btu/hr)
1485   IF Alt=(M,H)<Betag THEN Ppc=Ppc*Hpct
```

```
1490 Qa=Qu-Ppc                                    ! COLLECTOR ENERGY AVAILABLE
1495 IF (M=6) AND (H=1) THEN Qai=Qa               ! INSTANEOUS HEAT GAIN
1500 IF Qa<0 THEN GOTO N14                         ! WHEN PUMP REQ. > Q COLLECTED
1505 IF H>1 THEN Qa=2*Qa                           ! ALLOWS FOR DOUBLE SOLAR PERIOD
1510 ! Qtot - TOTAL USEFUL ENERGY OUT
1515 Qtot=Qtot+Qa
1520 Htot=Htot+(Hhid-1)*2+1                         ! TOTAL NUMBER OF HOURS
1525 IF Alts(M,H)<Betaq THEN GOTO N14
1530 N13: !----------------------------------------

1535                                        NEXT H
1540 !----------------
1545 N14: !------------
1550                                        NEXT M
1555 !---
1560 !---
1565 !---
1570 N15: !----- PERFORM AN ECONOMIC ANALYSIS ON THE SYSTEM -----
1575 !---
1580 !---
1585 !---
1590 Qyr=30*Qtot                                   ! YEARLY HEAT GAIN
1595 Ce=Qyr*Cf                                      ! FIRST YEAR FUEL SAVINGS
1600 Ir=Ia-If-Ia*If                                 ! EQUIVALENT ANNUAL INTEREST RATE
1605 Clc=Ce*((1+Ir)^Nyrs-1)/(Ir*(1+Ir)^Nyrs)
1610 Ci=Cac*L*(.8*At+.2*Cd)                         ! INITIAL COST ($/ft^3) COLLECTOR
1615 Ctot=Ci-Clc                                    ! TOTAL COST (-COST REP. SAVINGS)
1620 IF Qyr=0 THEN Qyr=1E-10
1625 Obj=Ctot/(Qyr+Nyrs)*1E6
1630 !
```

```
1635 '  -----------------------------              ----- CONSTRAINTS -----  ----------------------------
1640 N16: '
1645 '
1650 '
1655 O1=50000
1660 G(1)=Thetai-Thetat-3*PI/2                          ' MAXIMUM THETA-T
1665 G(2)=Thetai+PI/2-Thetat                            ' MINIMUM THETA-T
1670 G(3)=-(Mfr-1)*10
1675 G(4)=-(X(3)-.1)*10
1680 G(5)=1-Qtot/(2*O1)                                 ' MINIMUM AVERAGE DAILY HEAT GAIN
1685 G(6)=Tc21-600                                      ' MAXIMUM COLLECTOR TEMPERATURE
1690 IF Icalc=2 THEN GOTO N18
1695 '
1700 N17: '  .                                          ----- OUTPUT -----  ----------------------------
1705 '
1710 PRINTER IS 0
1715 IF Icalc=1 THEN PRINT "INITIAL DESIGN :"
1720 IF Icalc=3 THEN PRINT "FINAL DESIGN :"
1725 PRINT "FOR ";O1;" BTU/DAY SOLAR COLLECTOR"
1730 PRINT "DESIGN VARIABLES :"
1735 PRINT "     INCIDENT ACCEPTANCE ANGLE = ";X(1);" DEGREES"
1740 PRINT "     TRUNCATION ANGLE = ";X(2);" DEGREES"
1745 PRINT "     RECEIVER RADIUS = ";X(3);" INCHES"
1750 PRINT "     COLLECTOR LENGTH = ";X(4);" FEET"
1755 PRINT "     COOLANT MASS FLOW RATE = ";X(5);" Lbm/Hr "
1760 PRINT "DESIGN FEATURES :"
1765 PRINT "     CONCENTRATION RATIO = ";Cr
1770 PRINT "     COLLECTOR APERATURE AREA = ";At*L;" Ft^2"
1775 PRINT "     COLLECTOR DEPTH = ";Cd*12;" INCHES"
1780 PRINT "     COOLANT VELOCITY = ";Vc;" Ft/sec"
1785 PRINT "     MAXIMUM COOLANT TEMPERATURE = ";Tc21;" DEG F"
1790 PRINT "     INSTATANEOUS COLLECTOR EFFICIENCY = ";Qai/(At*L*279)
1795 PRINT "     AVERAGE DAILY HEAT GAIN = ";Qtot/2;" Btu"
1800 PRINT "     FIRST YEAR FUEL SAVINGS = $";Ce
1805 PRINT "     LIFE CYCLE FUEL SAVINGS = $";C1c
1810 PRINT "     INITIAL COST = $";Ci
1815 PRINT "     TOTAL LIFE CYCLE COST/ 1E6 Btu = $";Obj
1820 N18: ' END
1825 SUBEND
```

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APPENDIX H

Sample DESOP Output

Appendix H is a sample computer output for the DESOP program.

ANALIZE PROGRAM :   ROSEN

OPTIMIZER USED :   DESOP

INPUT FOR OPTIMIZATION :

NDV= 4   NCON= 3   IPRINT= 5   DELFUN= .001
DABFUN= .001   ITMAX= 20   IGNDIR= 5   FDCH= .0001
FDCHM= .0001   ABOBJ1= .1   ALPHAX= .1   IPDBG= 0
CT= .1   CTMIN=-.004   CTL= .1   CTLMIN=-.001
PHI= 5   THETA= 1   ITRM= 3   CG= 0
NCF= 0   IRMAX= 10   R2= 2   RMULT= 2
EXPG= 1.5   NSCAL= 1

X(1) = 1   X(2) = 1   X(3) = 1   X(4) = 1

VLB(1) = -1.0000000000000E+50   VUB(1) = 1.0000000000000E+50
VLB(2) = -1.0000000000000E+50   VUB(2) = 1.0000000000000E+50
VLB(3) = -1.0000000000000E+50   VUB(3) = 1.0000000000000E+50
VLB(4) = -1.0000000000000E+50   VUB(4) = 1.0000000000000E+50

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INITIAL DESIGN

DESIGN VARIABLES :
X(1)= 1   X(2)= 1   X(3)= 1   X(4)= 1

CONSTRAINTS :
G(1)=-4   G(2)=-6   G(3)=-1

OBJECTIVE FUNCTION :
OBJ= 31   OBJA= 31

OPTIMIZATION RESULTS

FINAL DESIGN VARIABLES :
X(1) = -5.166787812885E-03   X(2) = 1.019110574463
X(3) = 1.999501708832   X(4) = -.999510574088

FINAL CONSTRAINTS :
G(1)=-.002794556917   G(2)=-.9439983936   G(3)= .002320856596

FINAL OBJECTIVE FUNCTION :
OBJ= 6.006879126   OBJA= 5.999824765

NUMBER OF ITERATIONS : 28

NUMBER OF TIMES ANALIZE CALLED : 306

RZ HAS BEEN INCREASED 5 TIMES TO 64

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LIST OF REFERENCES

1. Kuester, J. L., and Mize, J. H., _Optimization Techniques_, PP. 73-74, 344-345, McGraw-Hill, 1973.

2. Himmelblau, D. M., _Applied Nonlinear Programming_, pp. 4-5, 42-44, McGraw-Hill, 1972.

3. Welford, W. T. and Winston, R., _The Optics of Nonimaging Concentrators: Light and Solar Energy_, pp. 5, 13, 50-52, 83-84, 92, 189-191, Academic Press, 1978.

4. _Solar Products Specification Guide_, Solar Age Magazine, Solar Vision Inc., 1980.

5. _ASHRAE Handbook of Fundamentals_, American Society of Heating Refrigeration and Air-Conditioning Engineers, Inc., pp. 386-399, 562-564, 669-681, 1972.

6. Kreith, F. and Kreider, J. F., _Principles of Solar Engineering_, pp. 59, 90-99, 208, 244, 264, 282-284, 509, 672, McGraw-Hill, 1978.

7. Vanderplaats, G. N., _COPES - A FORTRAN Control Program for Engineering Synthesis_, pp. 1-73, paper presented at the Naval Postgraduate School during the Engineering Design Optimization Course, 1980.

8. Vanderplaats, G. N., _Numerical Optimization Techniques for Engineering Design_, pp. 1-21, a paper presented at the Naval Postgraduate School during the Engineering Design Optimization Course, 1980.

9. NASA Technical Paper 1370, _Approximation Concepts for Numerical Airfoil Optimization_, pp. 2-5, by G. N. Vanderplaats, 1979.

10. Class notes from Engineering Design Optimization, a course given at the Naval Postgraduate School, 1980.

11. Kreider, J. F. and Kreith, F., _Solar Heating and Cooling: Engineering Practical Design and Economics_, pp. 246, 255, 258, McGraw-Hill, 1975.

12. ASHRAE Handbook of Equipment, American Society of
     Heating Refrigeration and Air-Conditioning Engineers,
     Inc.

13. Newnan, D. G., Engineering Economic Analysis, pp. 53,
     291-292, Engineering Press, 1976.

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